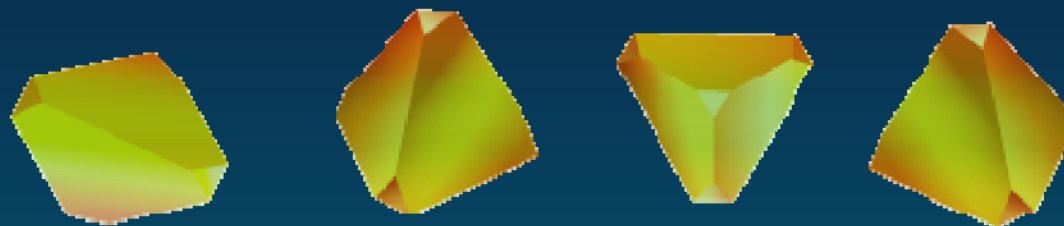


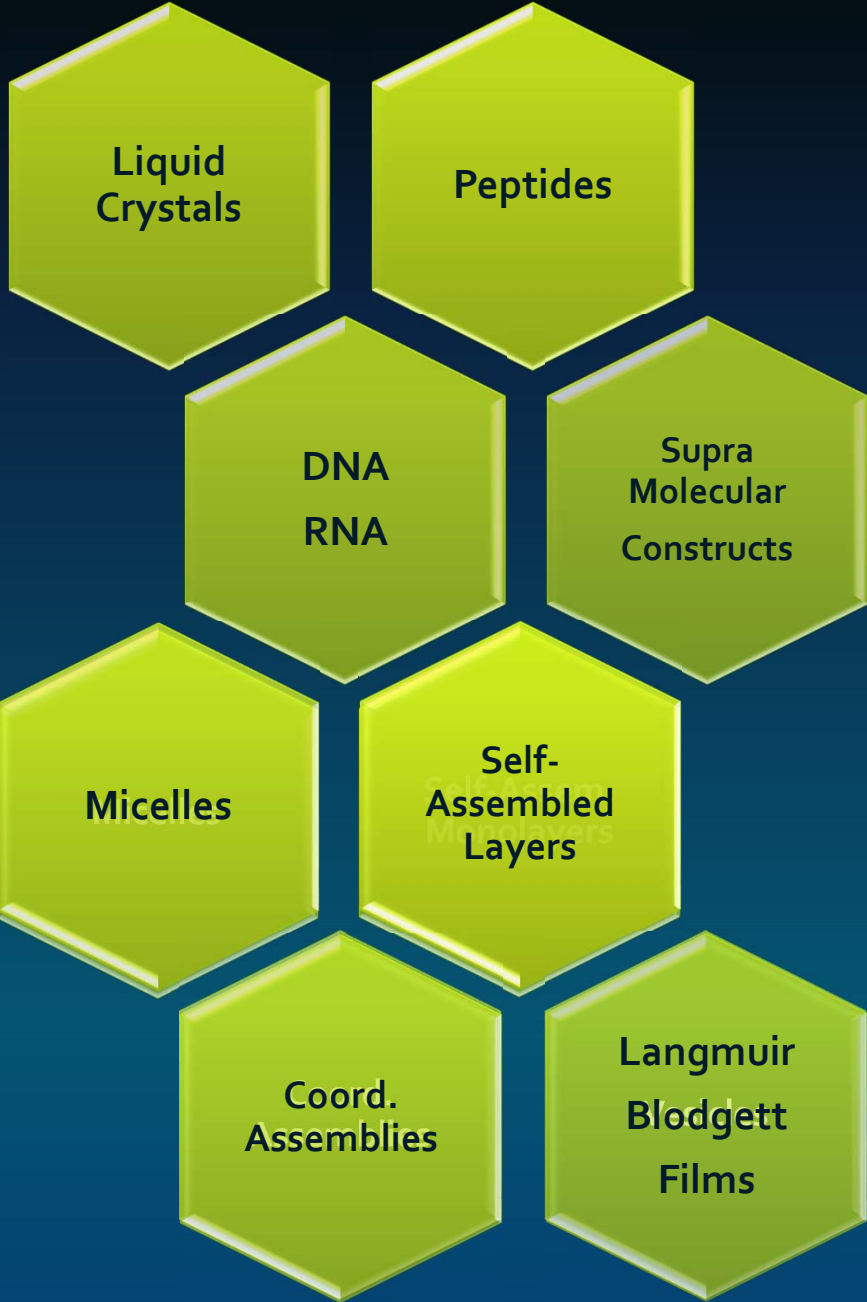


UNIVERSITY OF MICHIGAN, ANN ARBOR

# Hierarchical Assemblies of Inorganic Nanoparticles (NPs)



Nicholas A. Kotov



**Coordination bonds**

**Hydrophobic interaction**

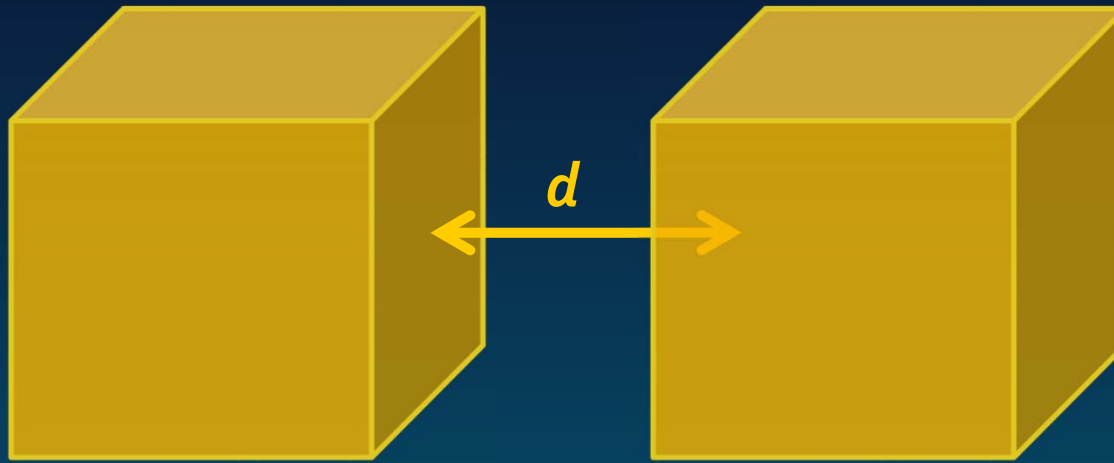
**van der Waals interactions**

**Electrostatic interactions**

**Covalent bonds**

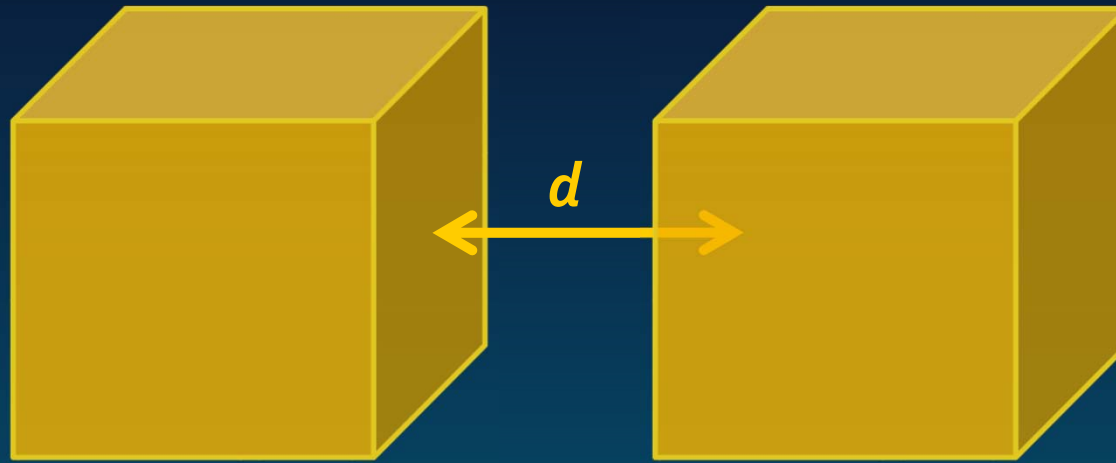
**Hydrogen Bonding**

# Interactions



London dispersion attraction  $V_{\text{LDF}} = A_{121}/12 \cdot \pi \cdot d^2$

# Interactions



$A_{121}$

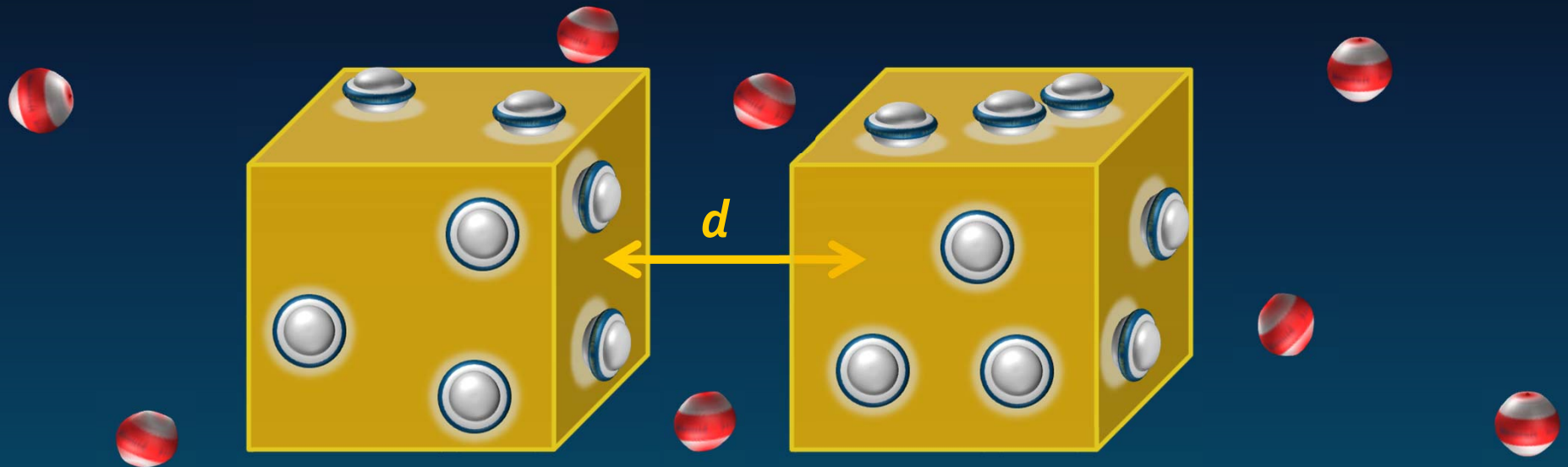
Metals and semiconductors

$10 - 40 \cdot 10^{-20} \text{ J}$

Organic molecules

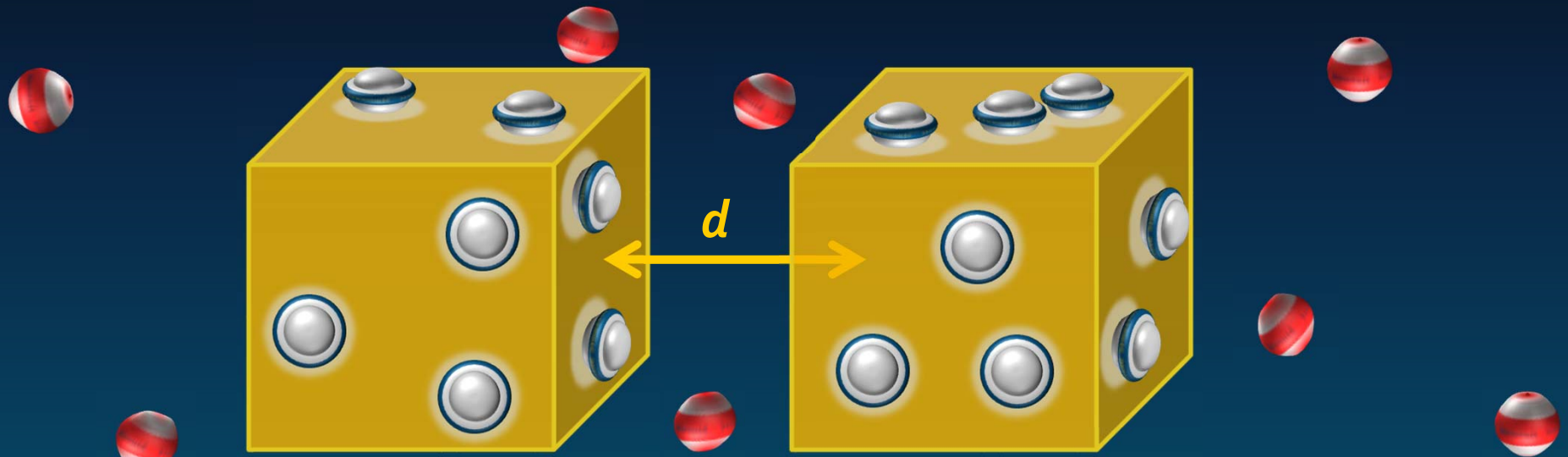
$1 - 10 \cdot 10^{-20} \text{ J}$

# Interactions



Electrostatic Repulsion: 
$$V_{EL} = \frac{64 \cdot kT \cdot \sigma_0}{\epsilon_0 \epsilon} \exp(-\kappa_D d)$$

# Interactions



$\sigma_0$

Metals and semiconductors

1 — 60 mC/m<sup>2</sup>

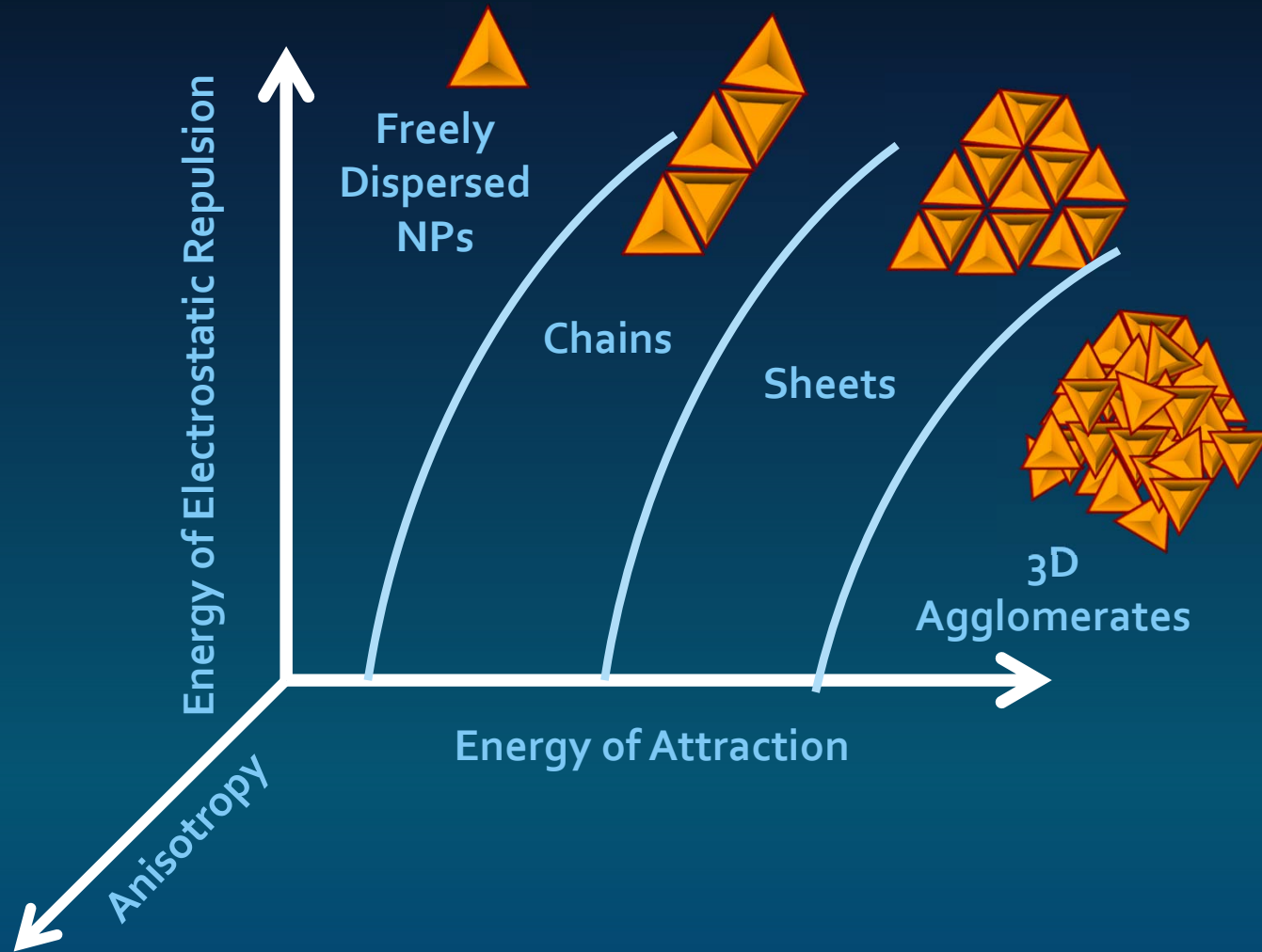
Organic materials, insulators

26 — 100 mC/m<sup>2</sup>

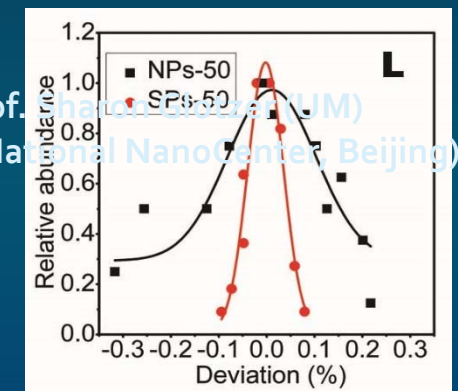
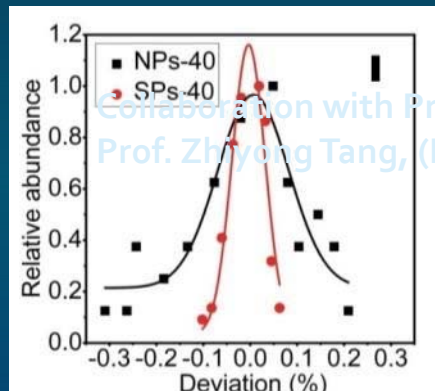
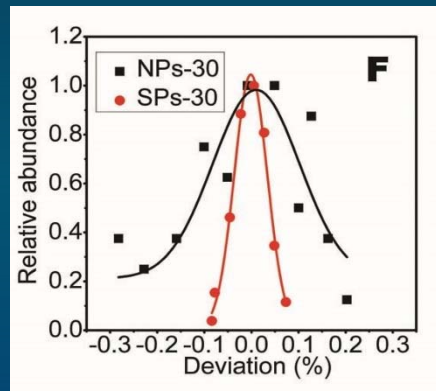
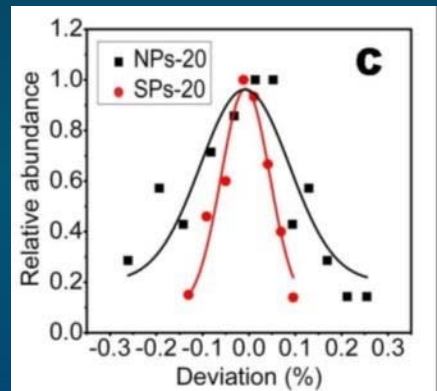
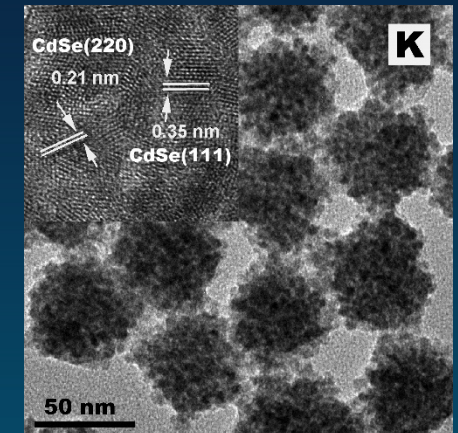
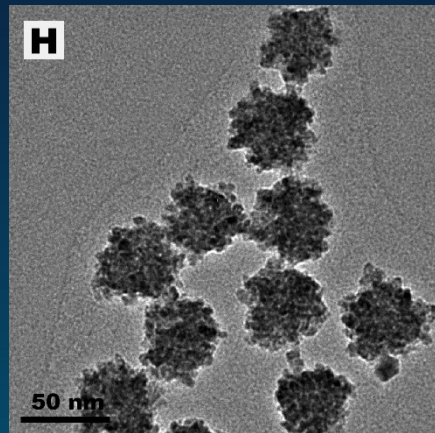
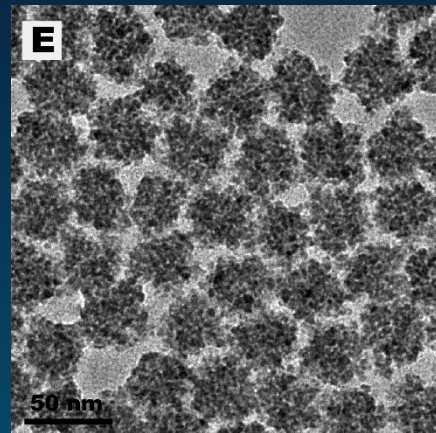
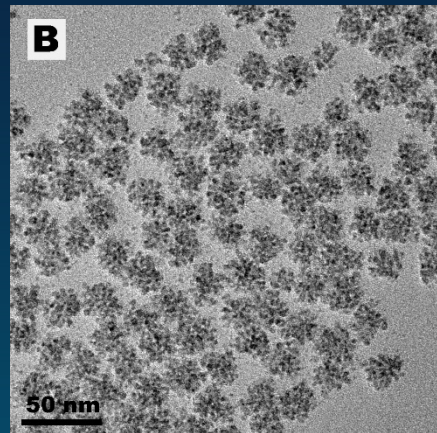
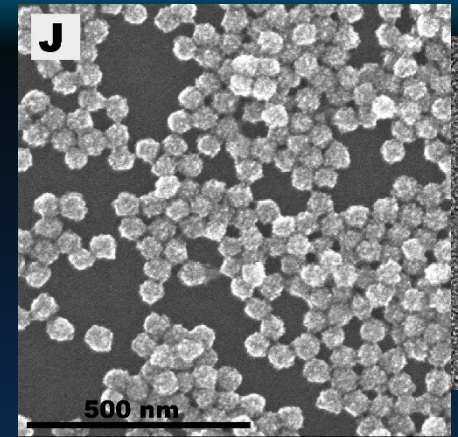
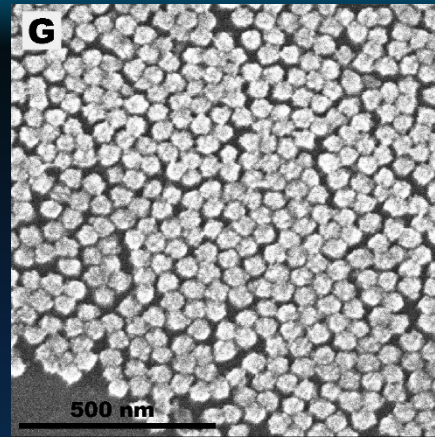
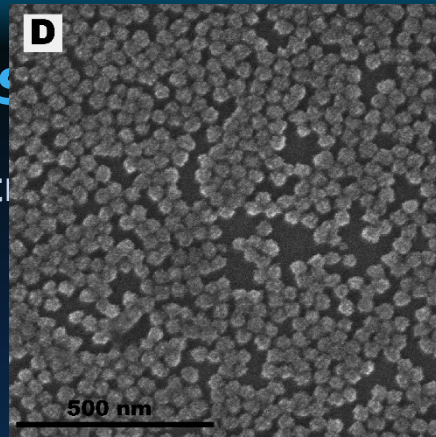
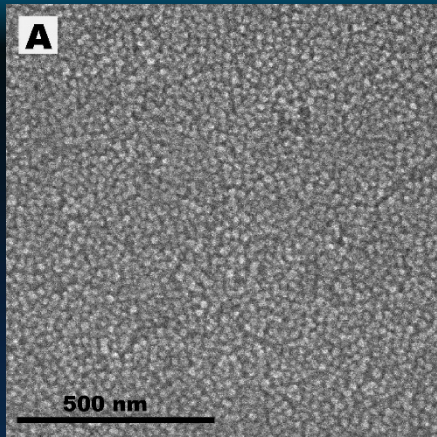
# Simplicity

Wide range of experimental conditions and building blocks

# Simple Phase Diagram



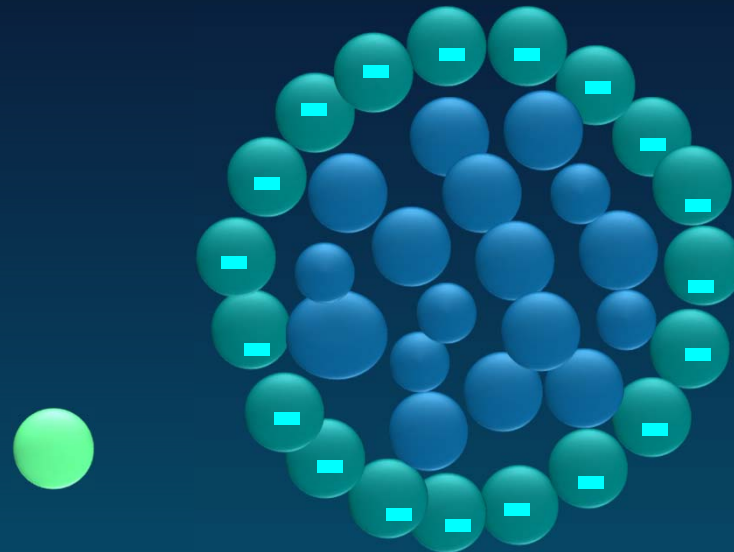
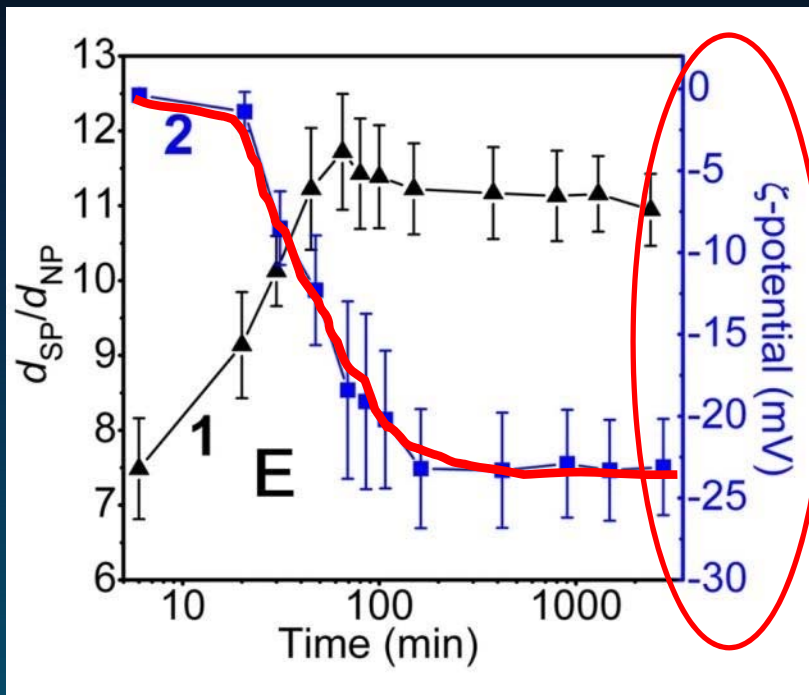




Collaboration with Prof. Zhenhai Zhang (JNU)  
 Prof. Zhiyong Tang, (National Nanocenter, Beijing)

Y. Xia, T. D. Nguyen, M. Yang, B. Lee, A. Santos, P. Podsiadlo, Z. Tang, S. C. Glotzer, N. A. Kotov,  
 Self assembly of virus-like self-limited inorganic supraparticles from nanoparticles, *Nature Nanotechnology*, 2011, 6, 580

# Mechanism of Supraparticle Self-Assembly

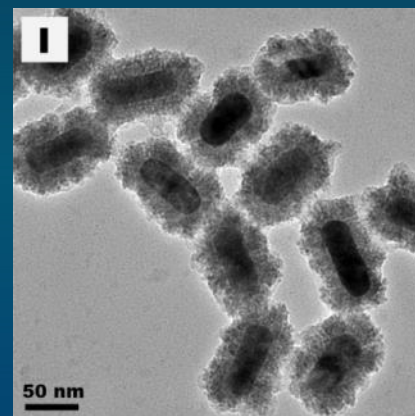
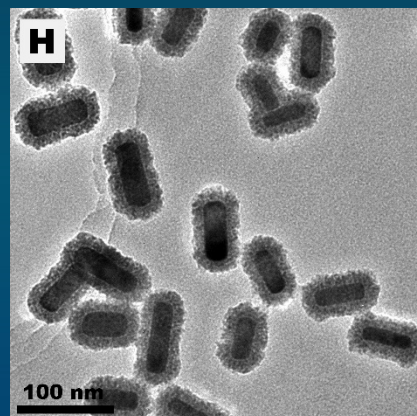
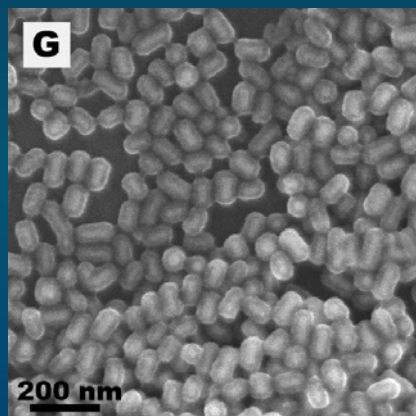
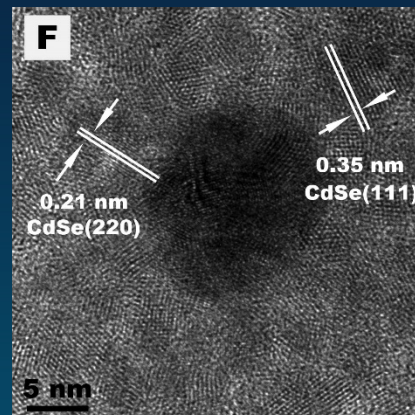
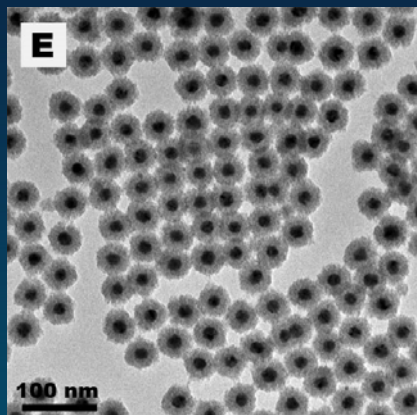
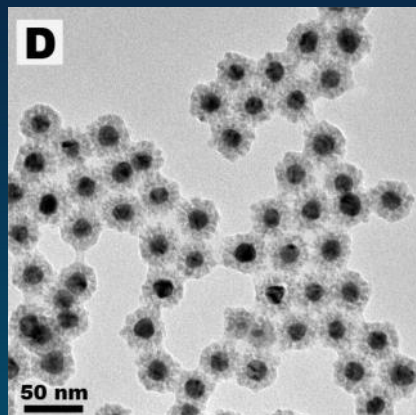
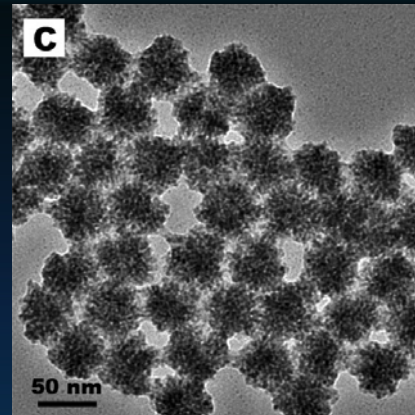
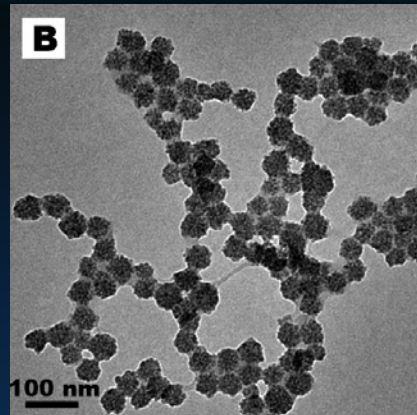
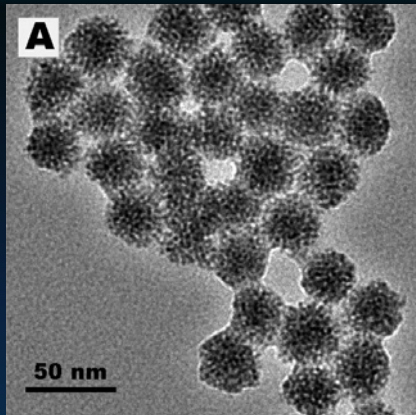


Supraparticle is formed due to balance of electrostatic repulsion and London dispersion attraction.

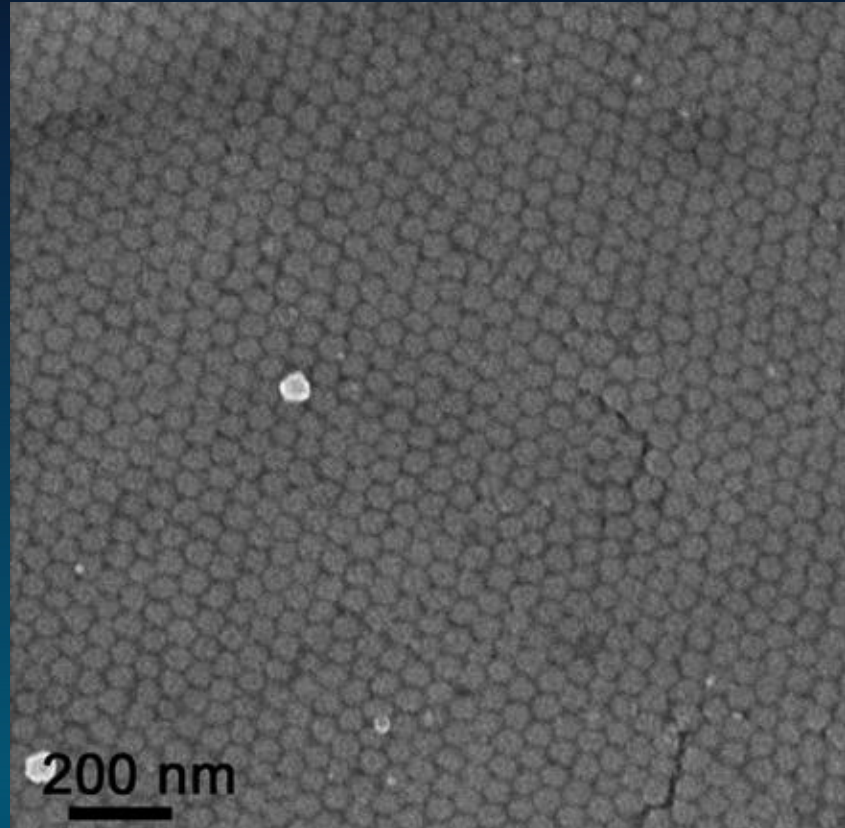
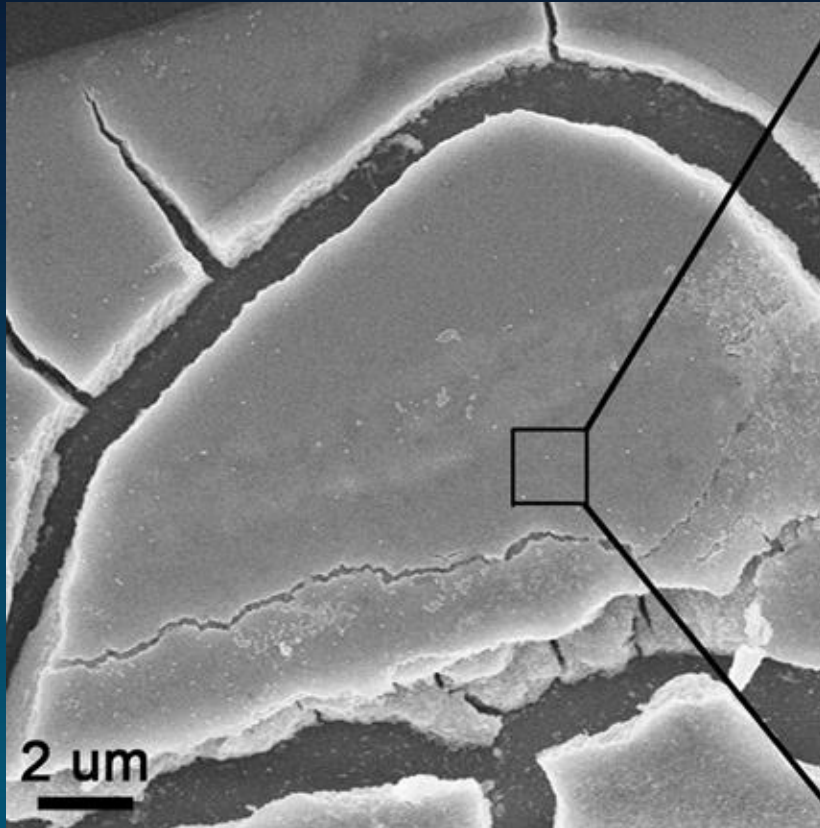
Other Assemblies  
CdSe, PbS, PbSe

Complex Assemblies  
with **Au NP**  
in the center

Complex Assemblies  
with **Au NanoRods**  
in the center



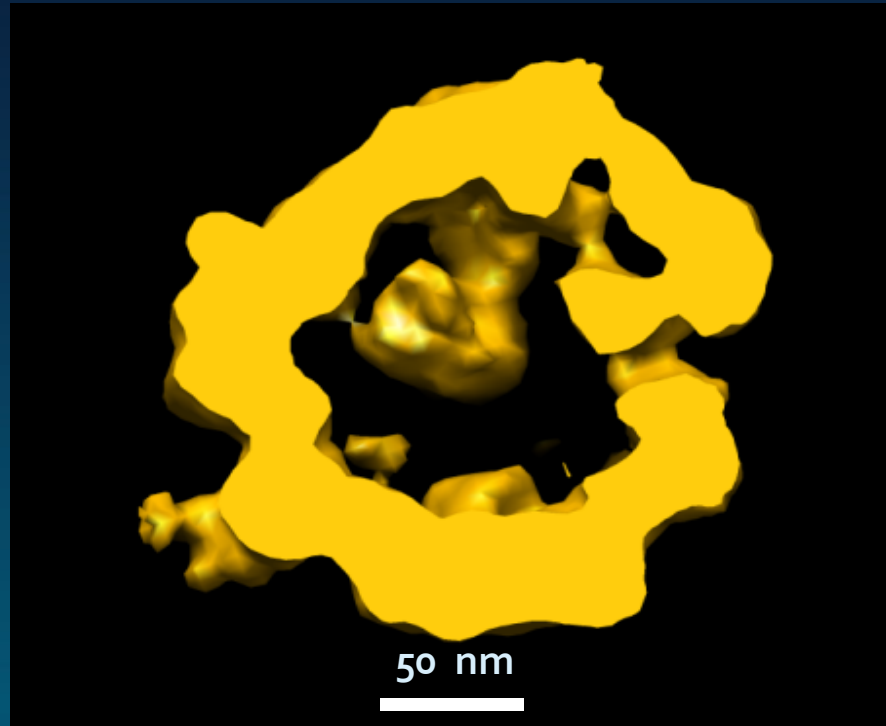
# Colloidal Crystals from Supraparticles



Assembly combining the nanoscale and mesoscale structural motifs

# Capsid-Like Biomimetic Nanoshells

Collaborations with  
Prof. Petr Král, U. Illinois Chicago  
Prof. Peijun Zhang, U. Pittsburg



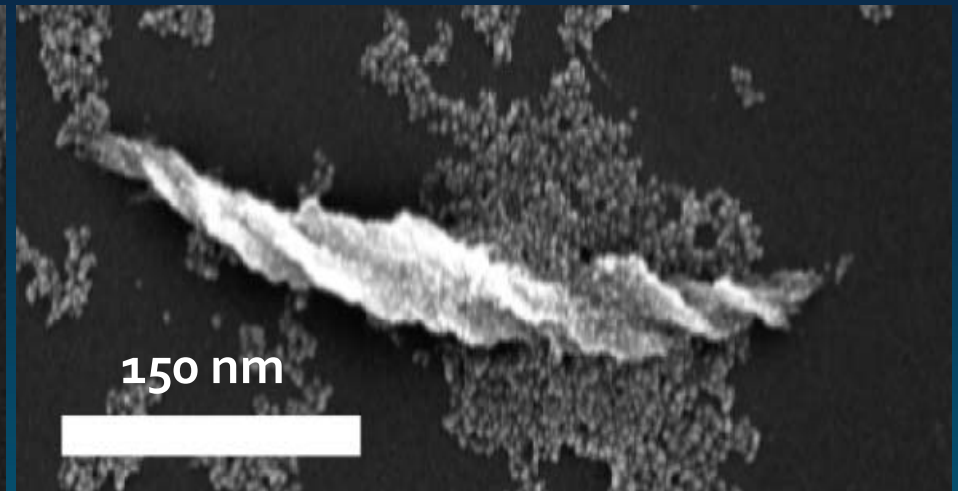
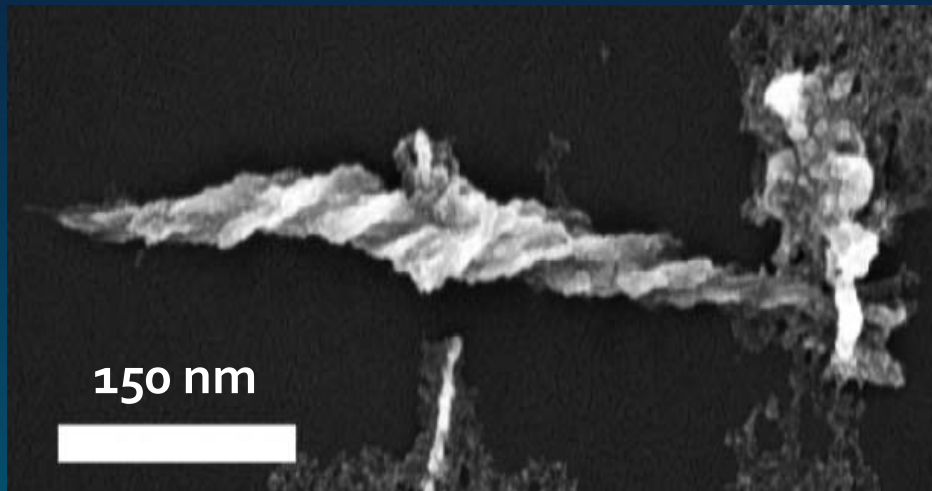
Cryo-TEM  
Tomography

M. Yang, H. Chan, G. Zhao, J.H. Bahng, P. Zhang, P.Král, N. A. Kotov, Self-Assembly of Nanoparticles into Biomimetic Capsid-Like Nanoshells, *Nature Chemistry*, 2017, 9, 287–294.

# Assemblies of Chiral NPs into Nanohelices

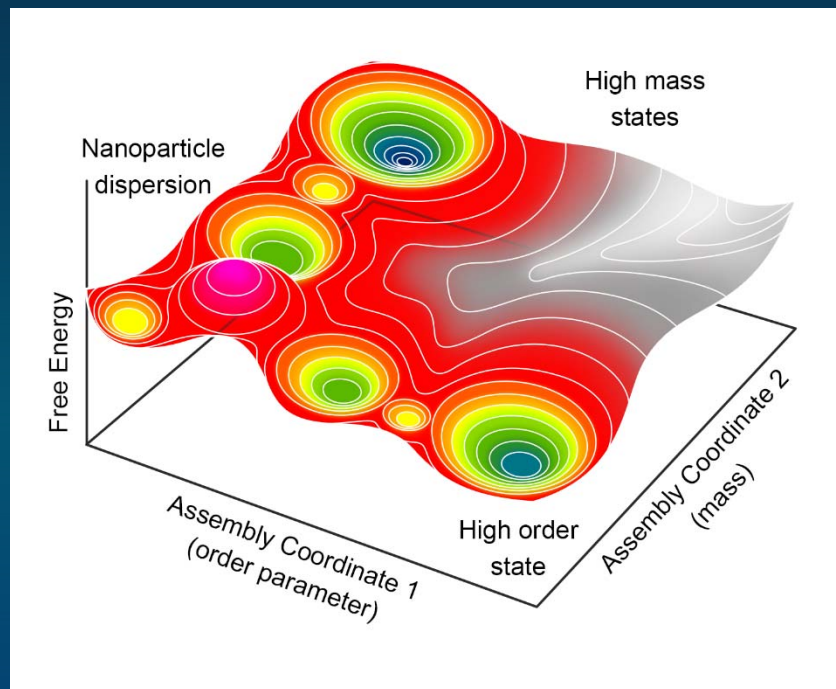
CdTe NP stabilized with D-CYS

CdTe NP stabilized with L-CYS



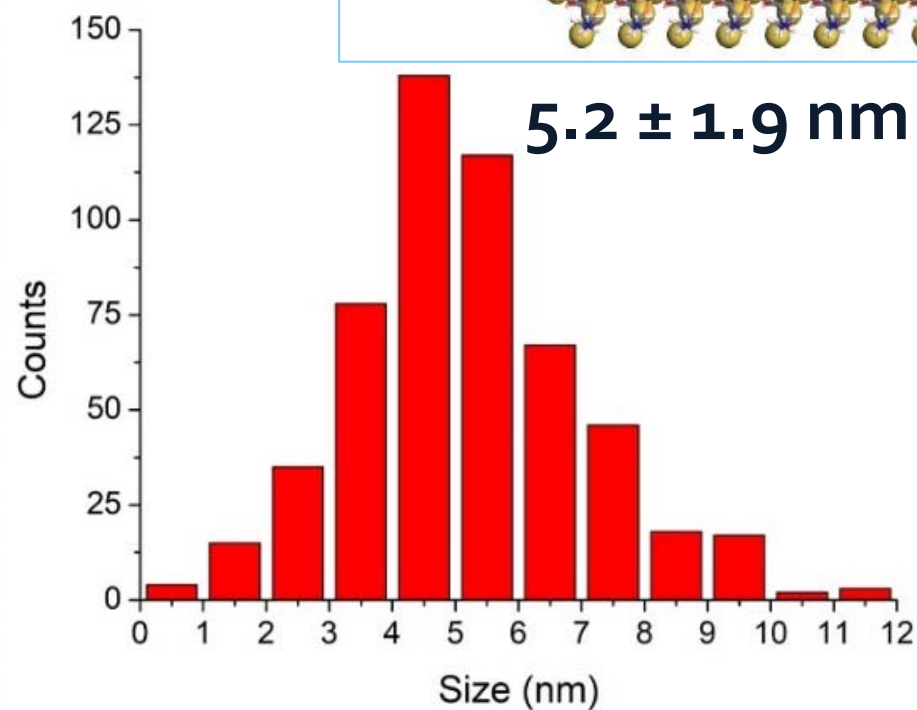
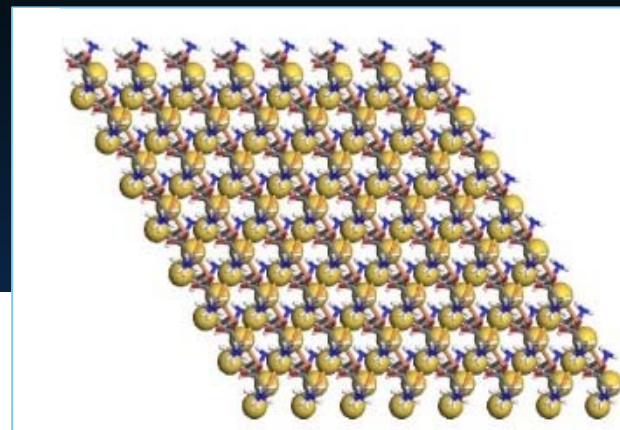
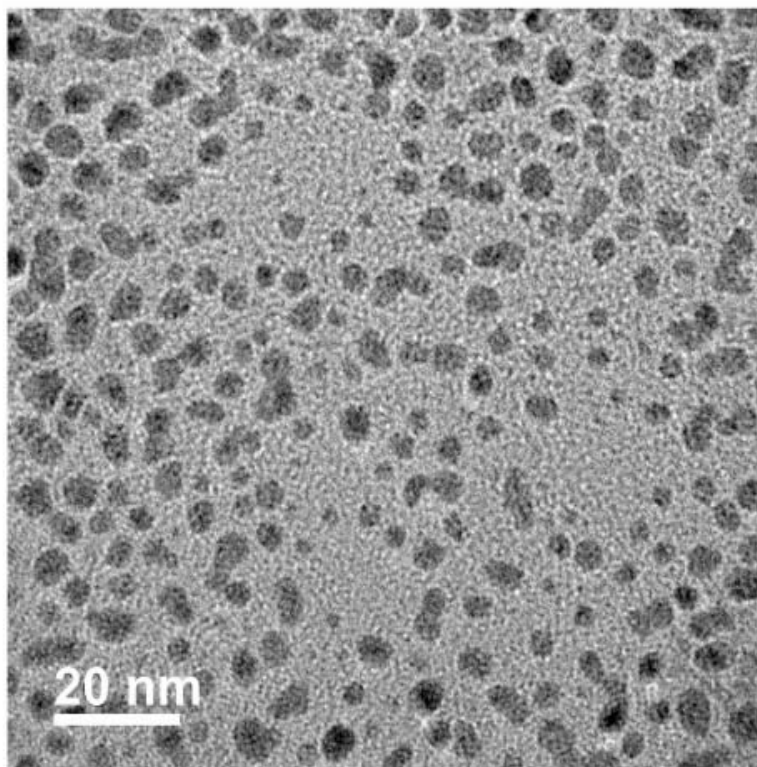
J. Yeom, B. Yeom, H. Chan, K.W. Smith, S. Dominguez-Medina, J.H. Bahng, G. Zhao, W.-S. Chang, S.J. Chang, A. Chuvilin, D. Melnikau, A.L. Rogach, P. Zhang, S. Link, P. Král, N. A. Kotov, *Nature Materials*, 2015, 14, 66–72

# Does self-assembly of complex systems require monodispersity?



Energy landscape  
of self-assembly

# Polydispersed Building Blocks Au-S nanosheets

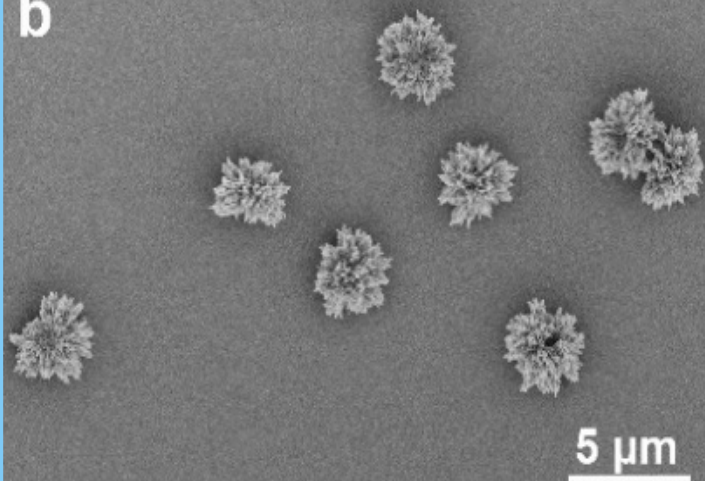




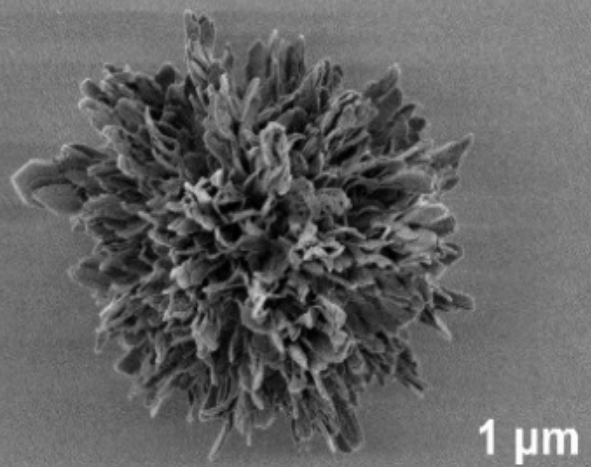
# Self-Assembled Chiral Hedgehog Particles

Au-D-Cys SPs

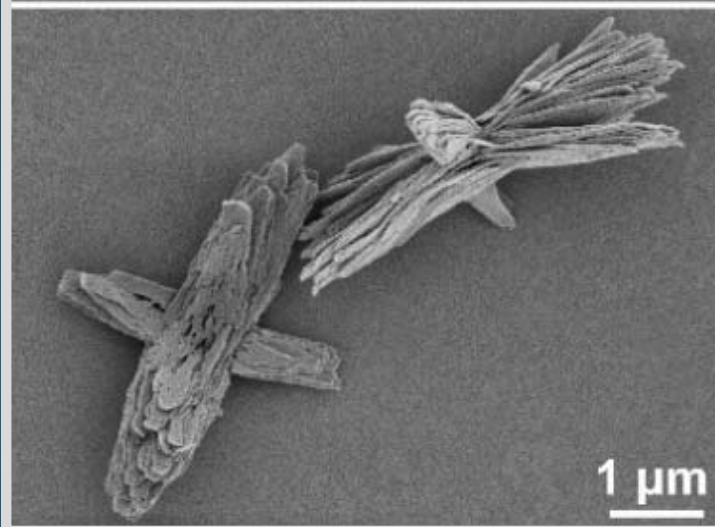
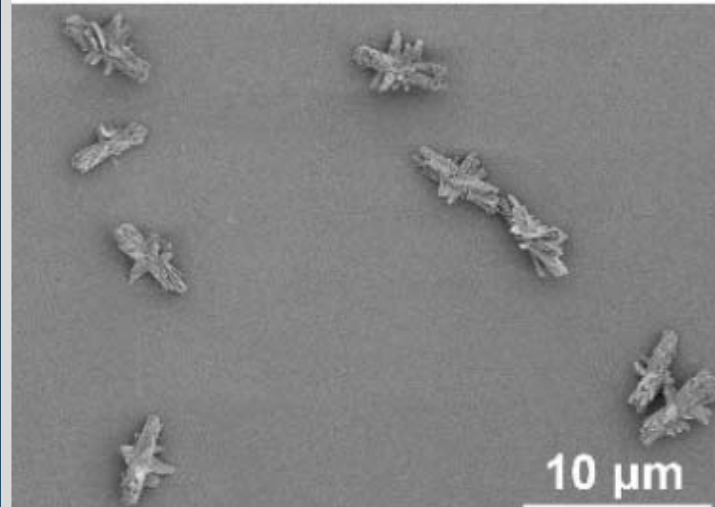
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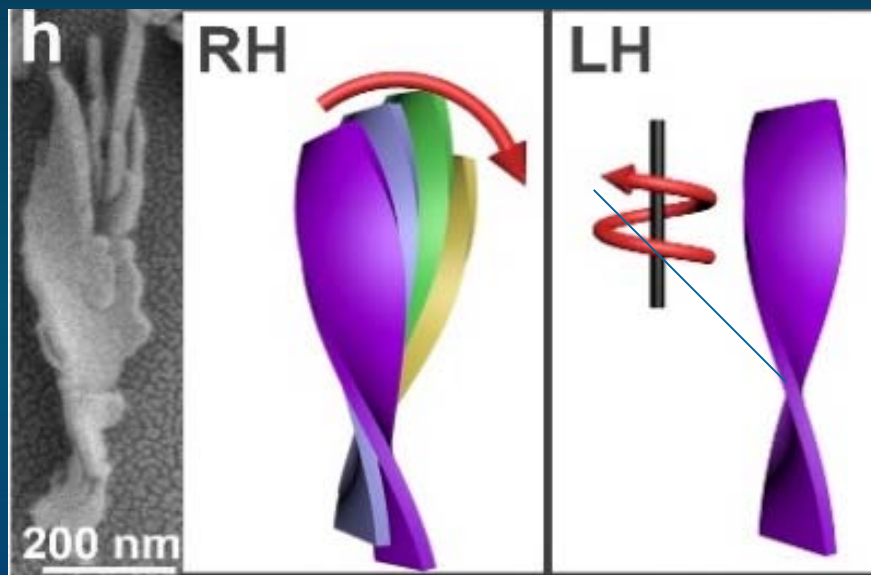
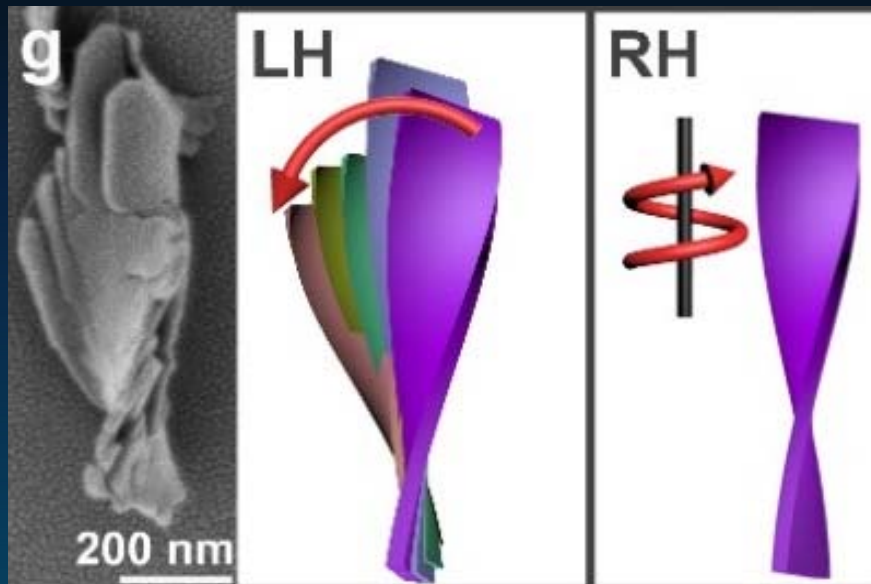
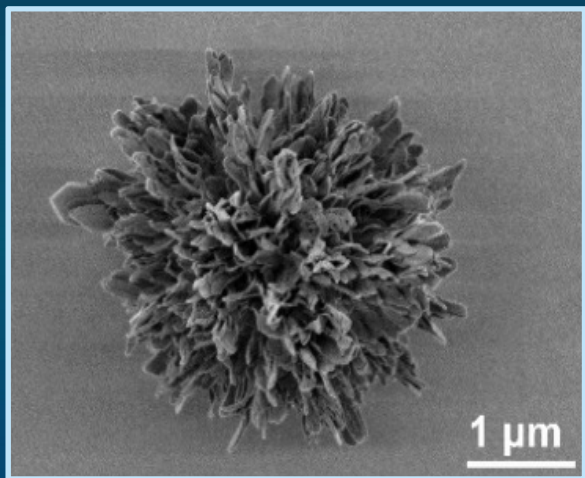
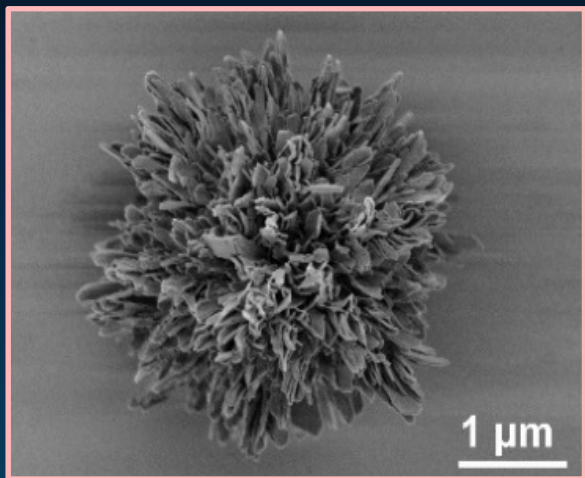
e



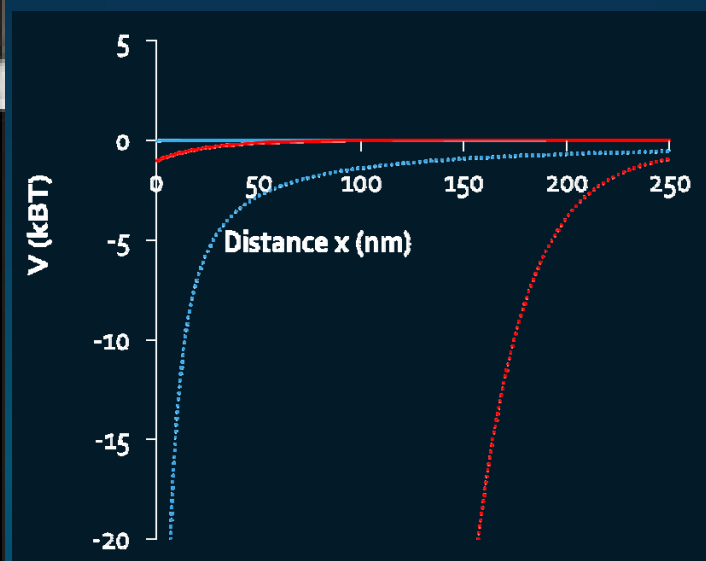
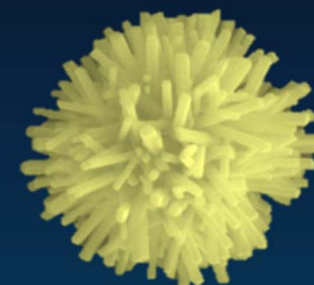
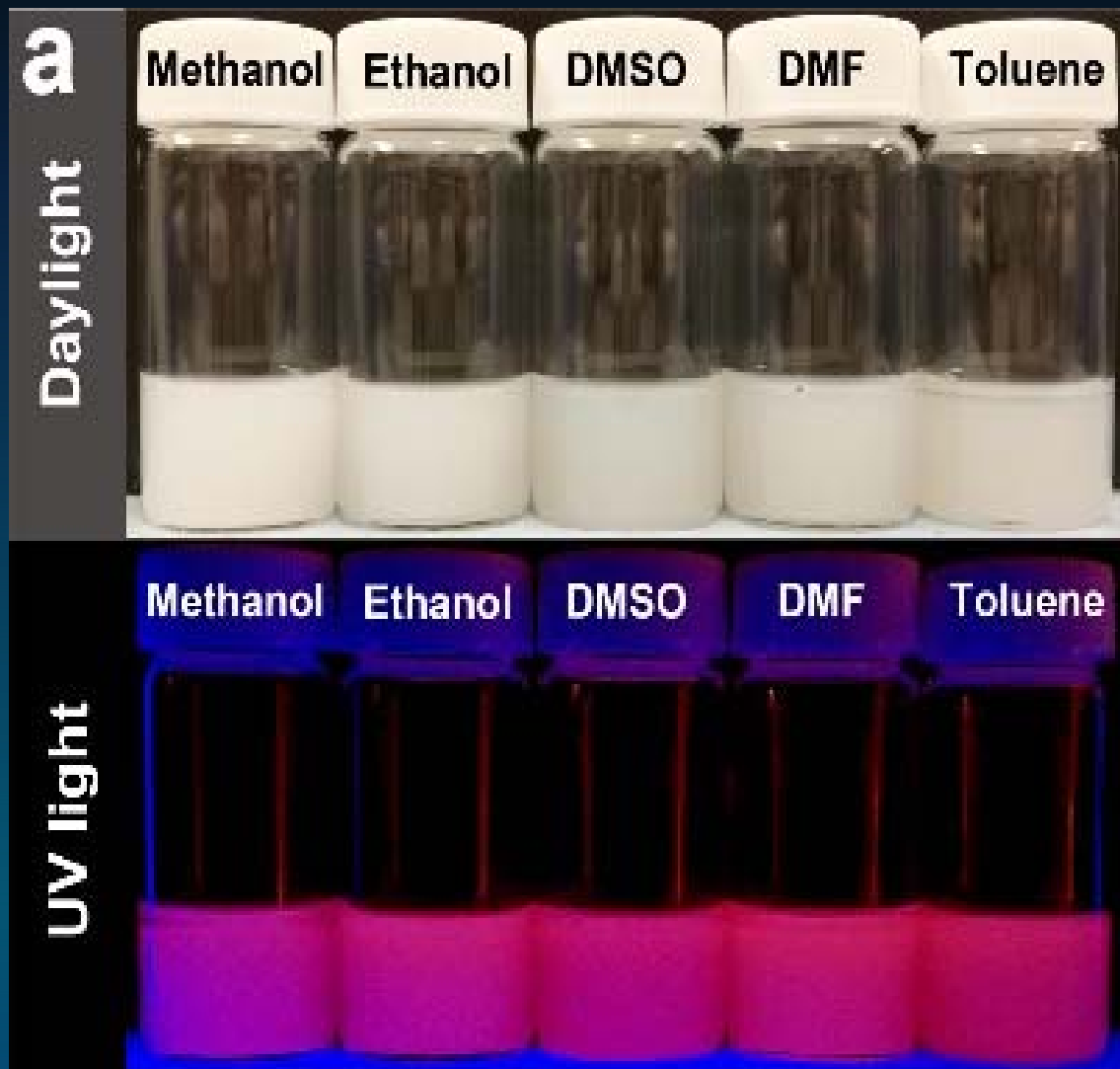
Au-DL-Cys SPs



# Chiroptically Active Hedgehog Particles

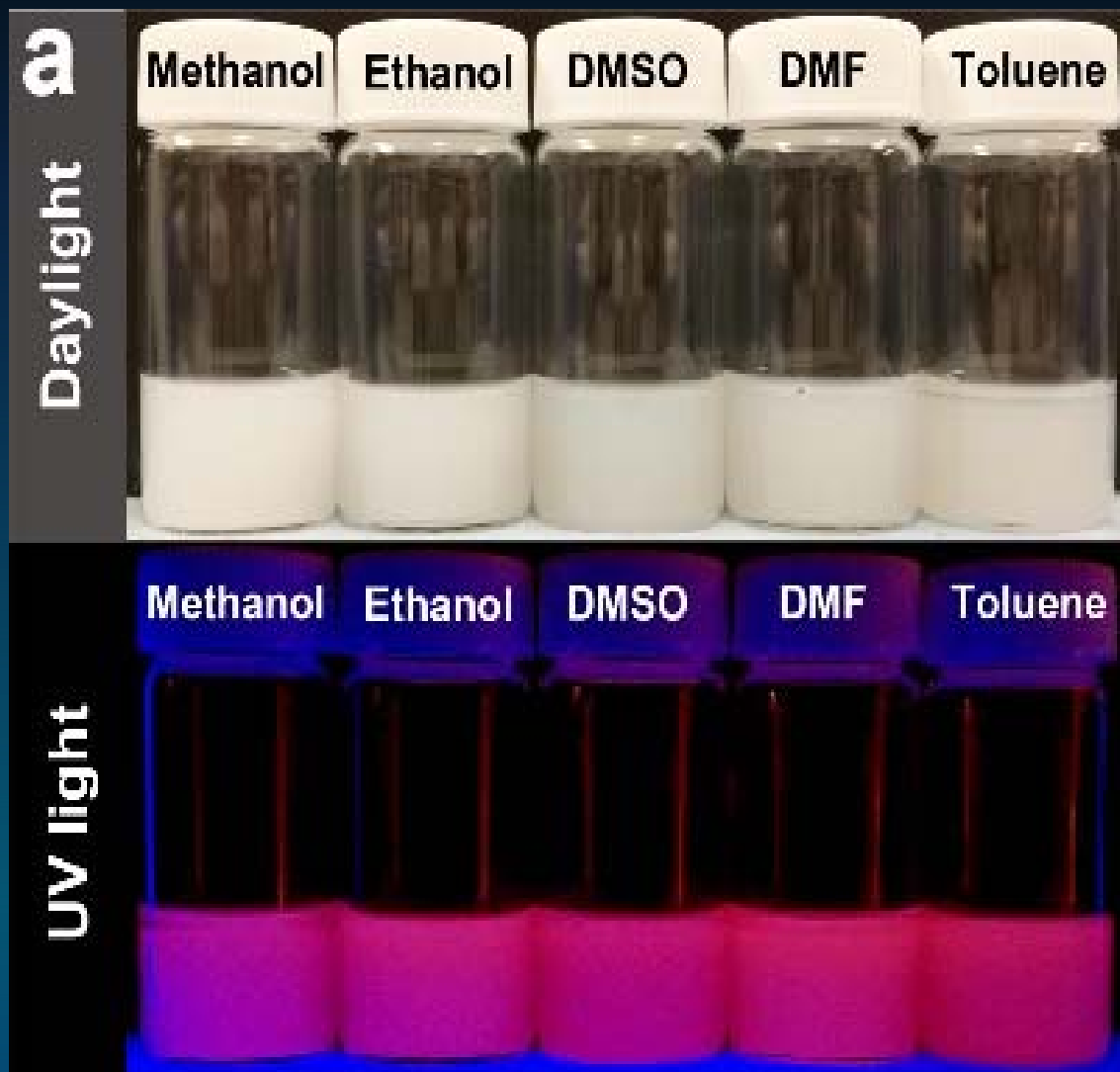


# Self-Assembled Hedgehog Particles



J. H. Bang, B. Yeom, Y. Wang, S. O. Tung, N.A. Kotov, Anomalous Dispersions of Hedgehog Particles, *Nature*, 2015, 517, 596

# Self-Assembled Hedgehog Particles



Au-S  
2D  
Material

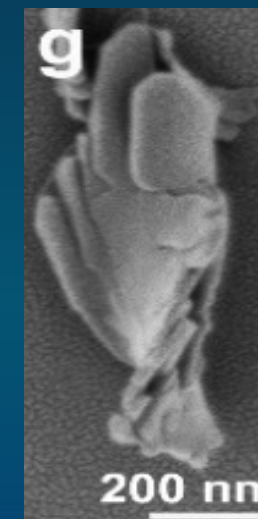
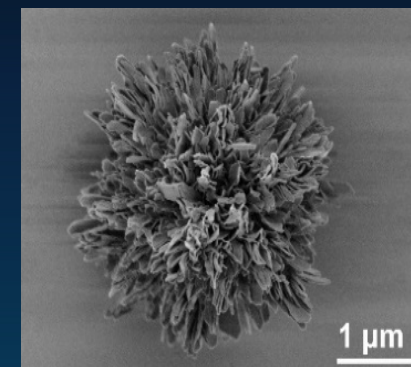
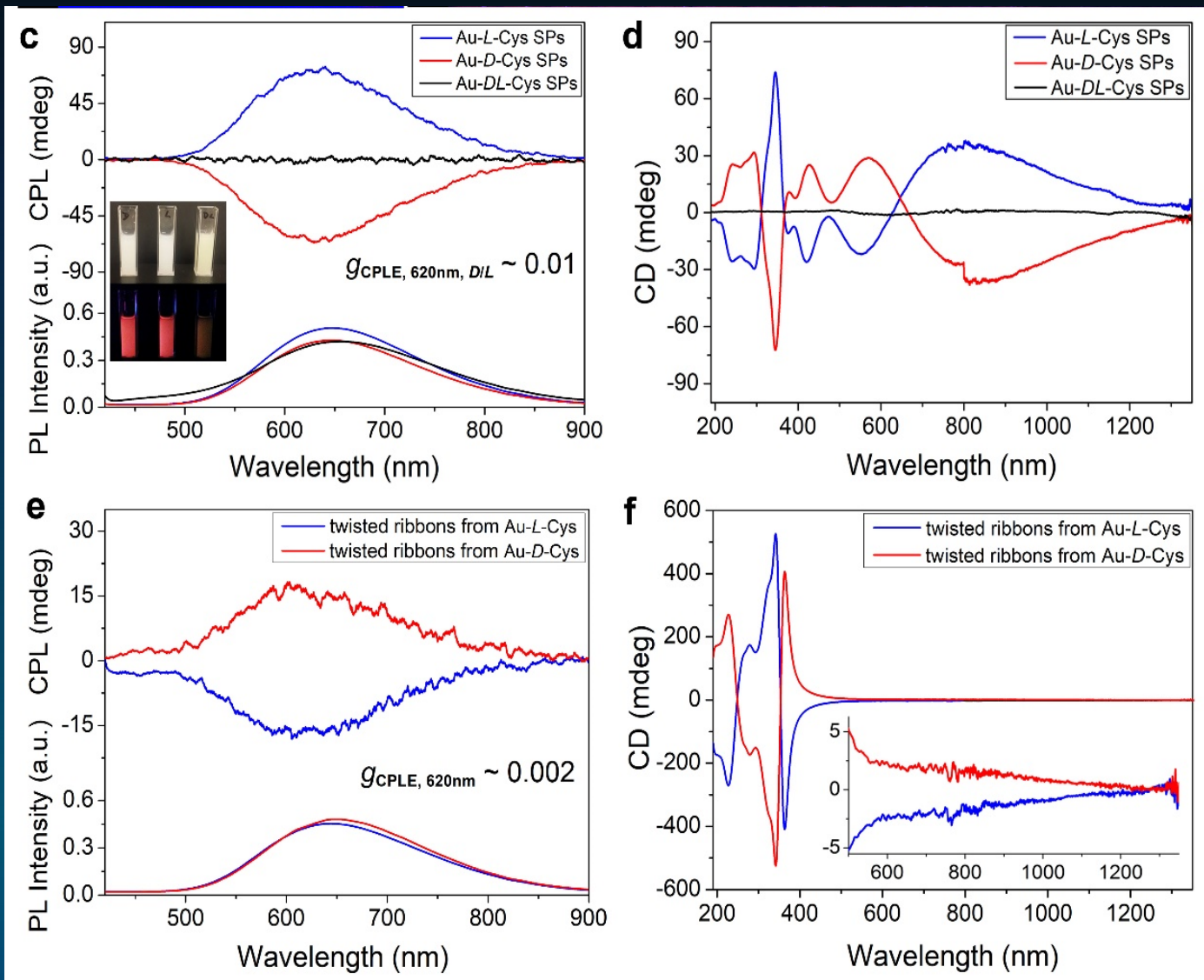
Strong  
Optical  
Emission

Jiang, W.; Qu, Z.; Kumar, P.; Vecchio, D.; Wang, Y.; Ma, Y.; Bahng, J. H.; Bernardino, K.; Gomes, W. R.; Colombari, F. M.; *et al.* Emergence of Complexity in Hierarchically Organized Chiral Particles. Second revision

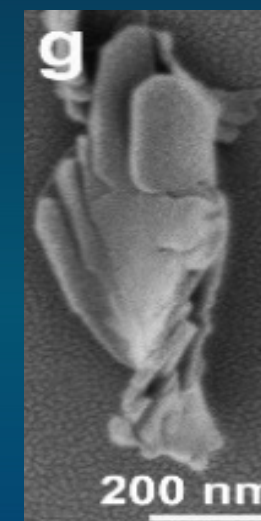
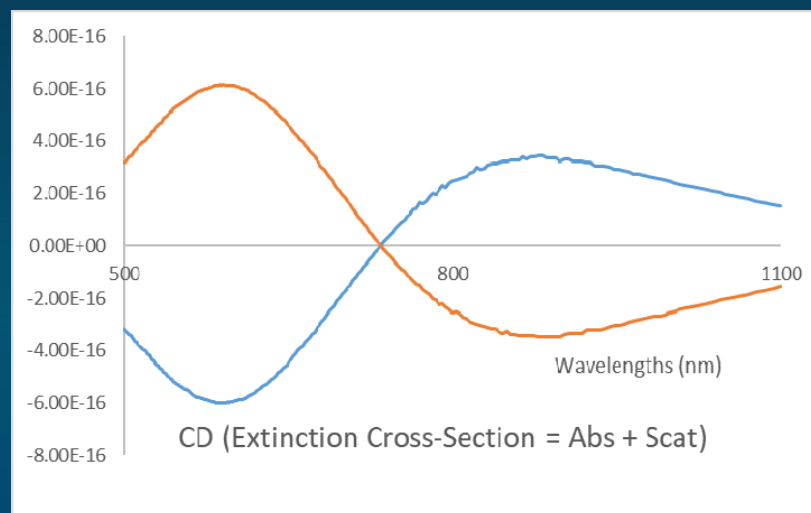
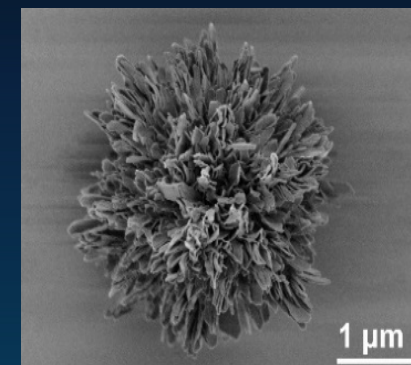
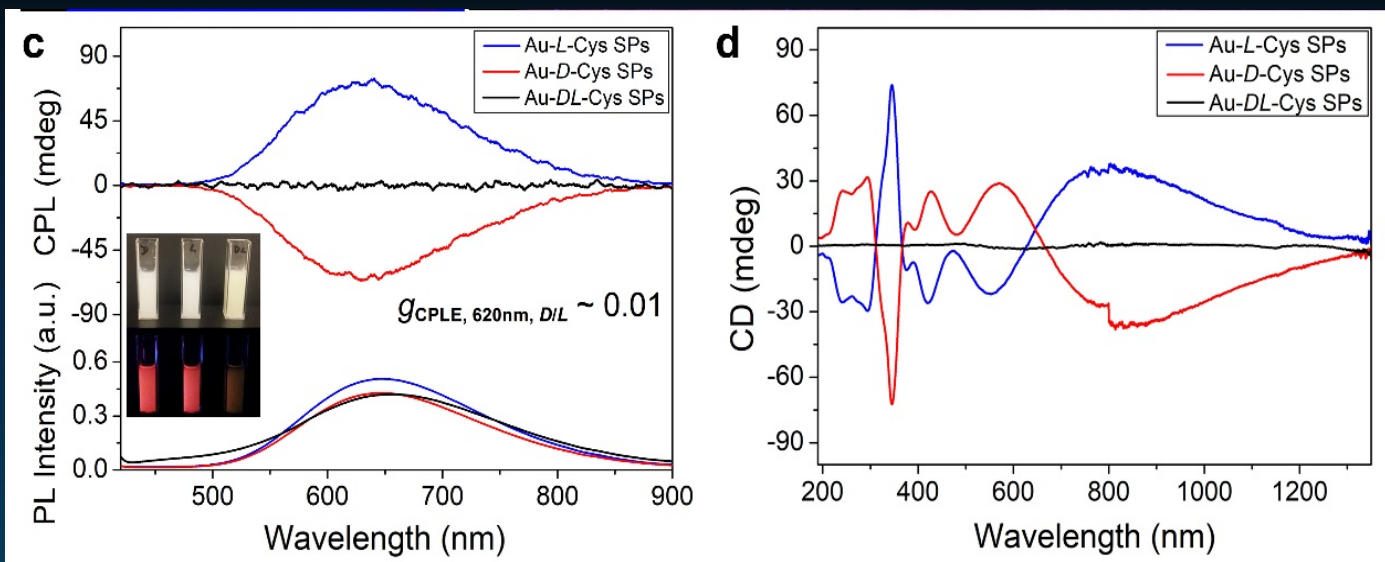
# Unusual pH Stability



# Chiroptically Active Hedgehog Particles



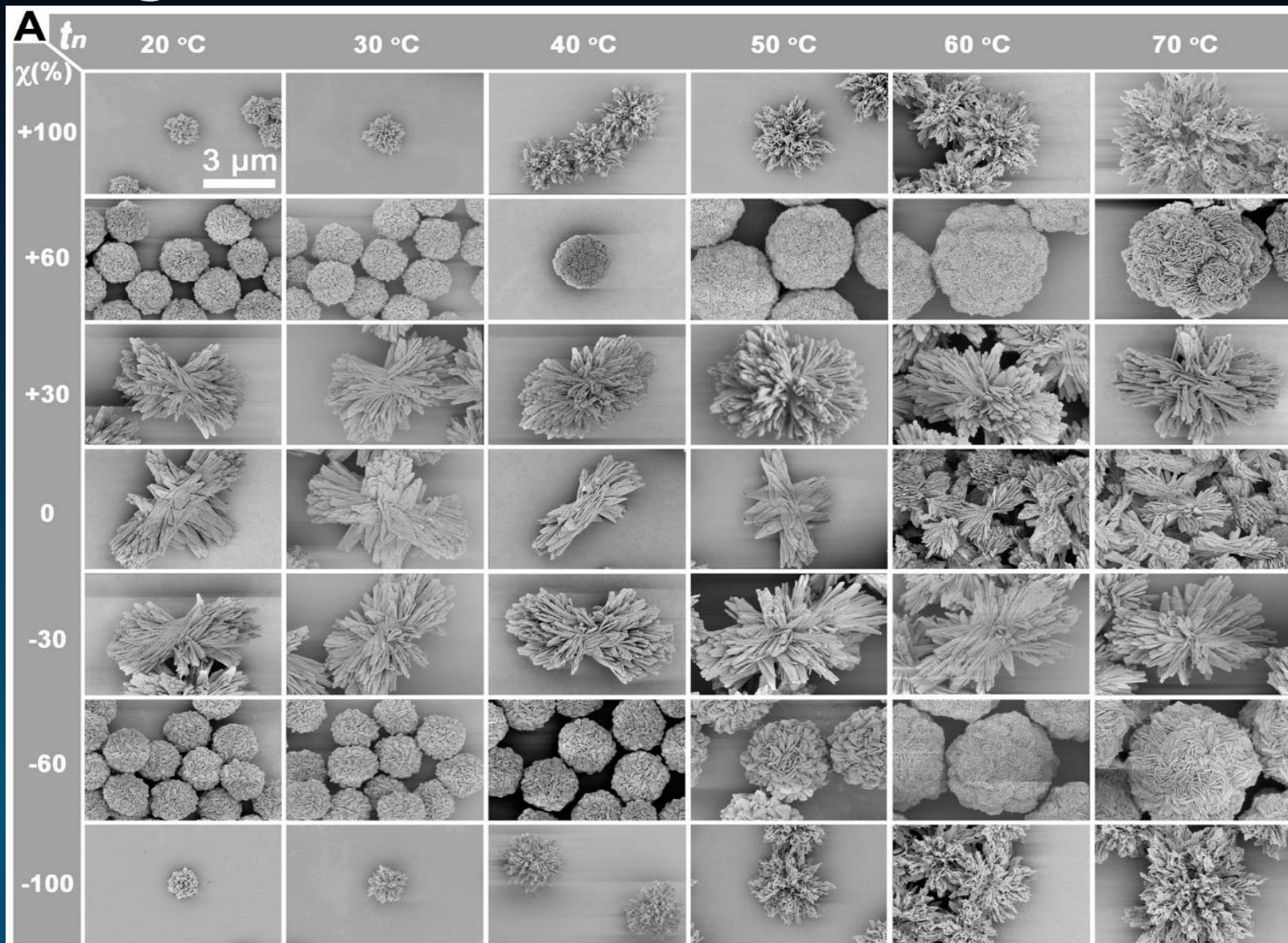
# Chiroptically Active Hedgehog Particles



# Phase diagram

Temperature, deg °C

Chirality, e.e.%

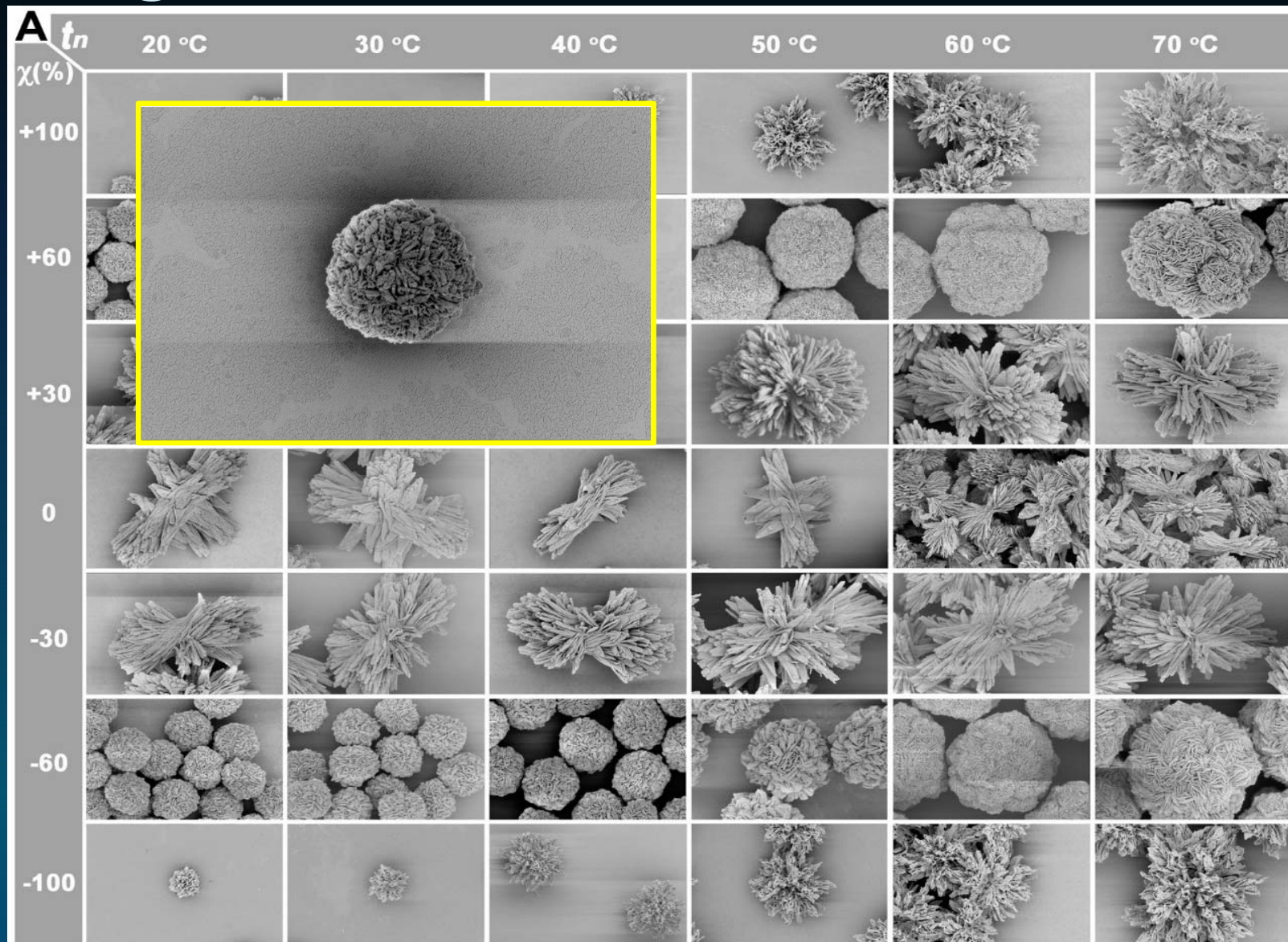




# Phase diagram

Temperature, deg °C

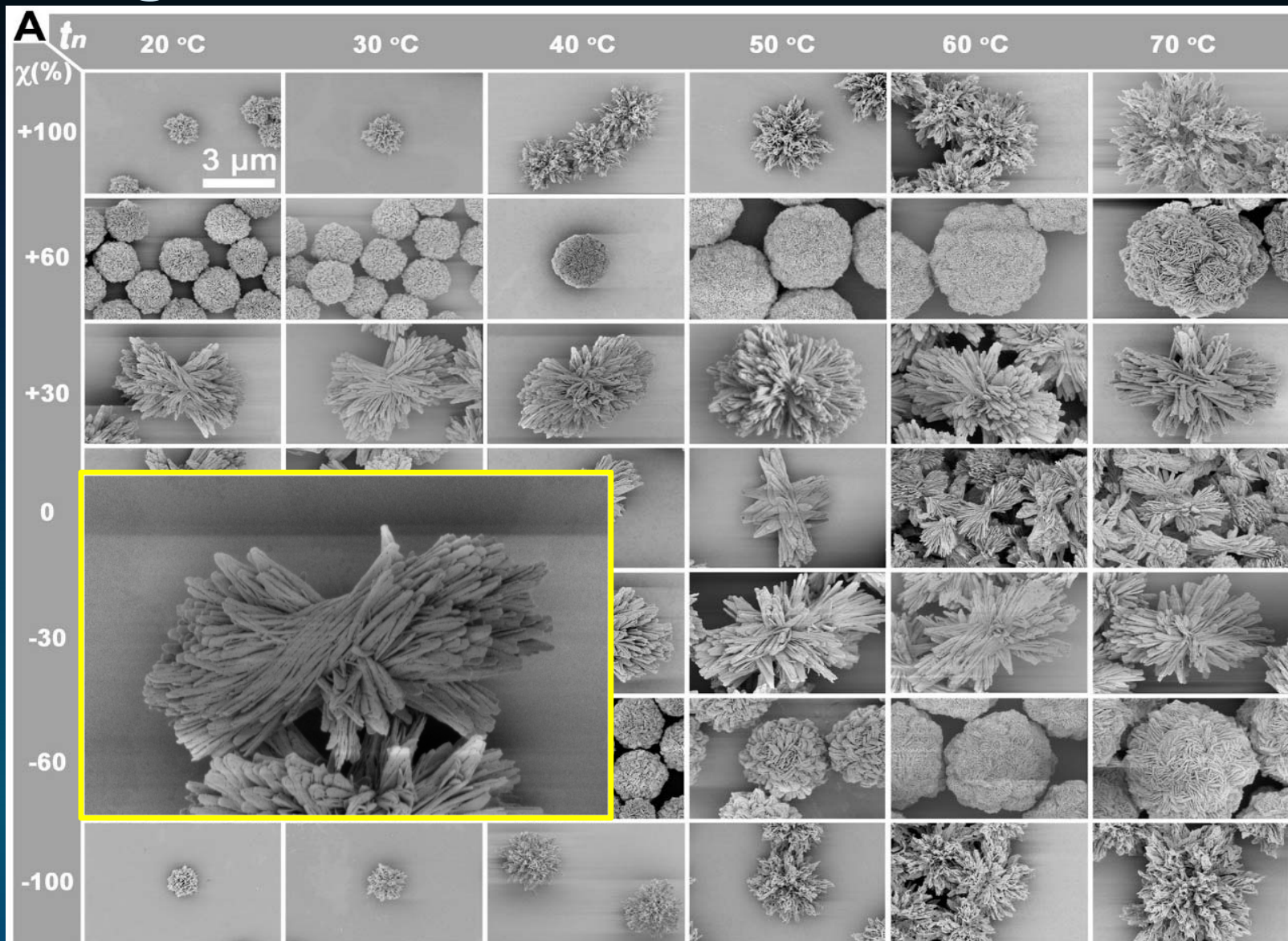
Chirality, e.e.%



# Phase diagram

Temperature, deg °C

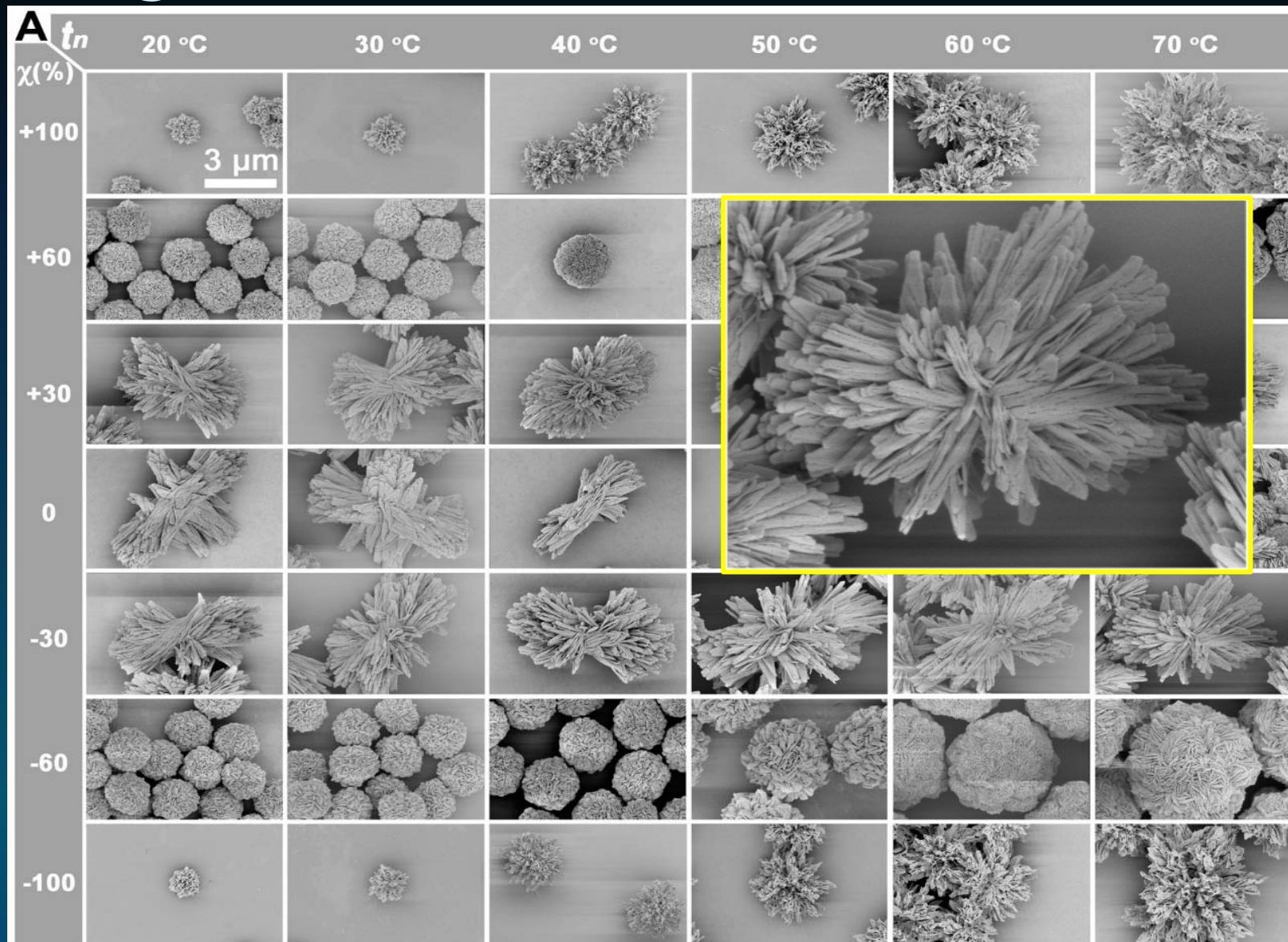
Chirality, e.e.%



# Phase diagram

Temperature, deg °C

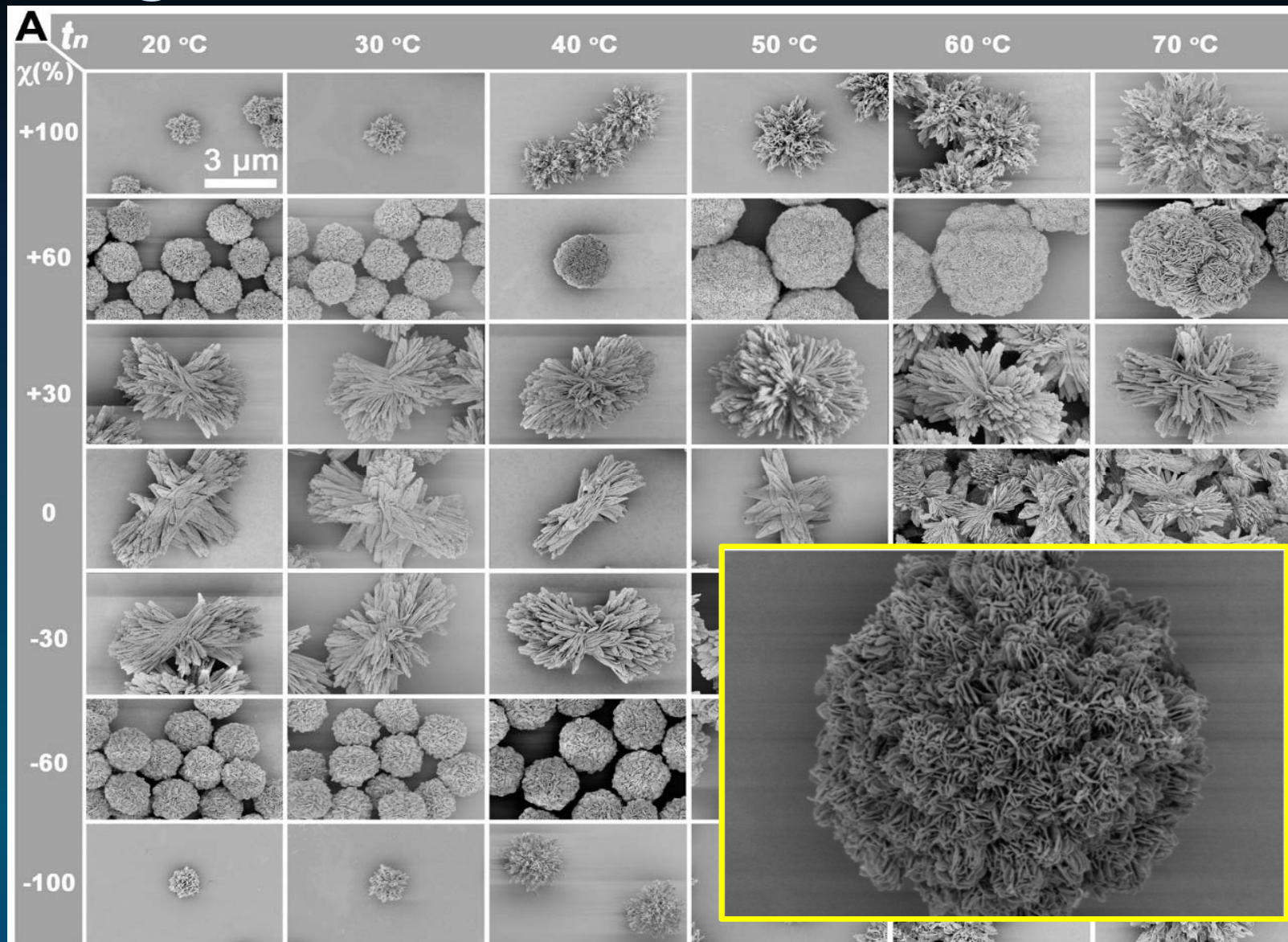
Chirality, e.e.%



# Phase diagram

Temperature, deg °C

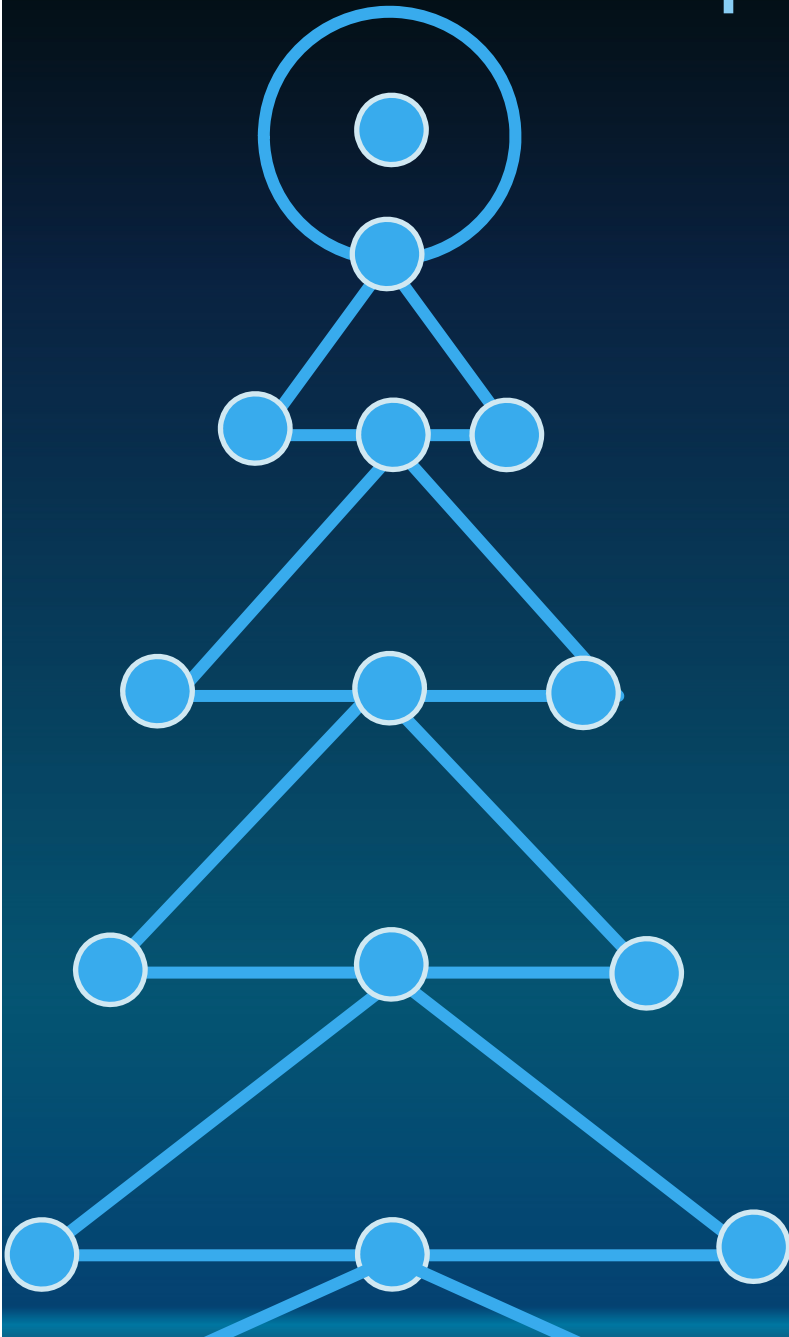
Chirality, e.e.%



# Graphs and Complexity

**GRAPH** - a set of nodes  
and edges

**COMPLEXITY** - information  
content



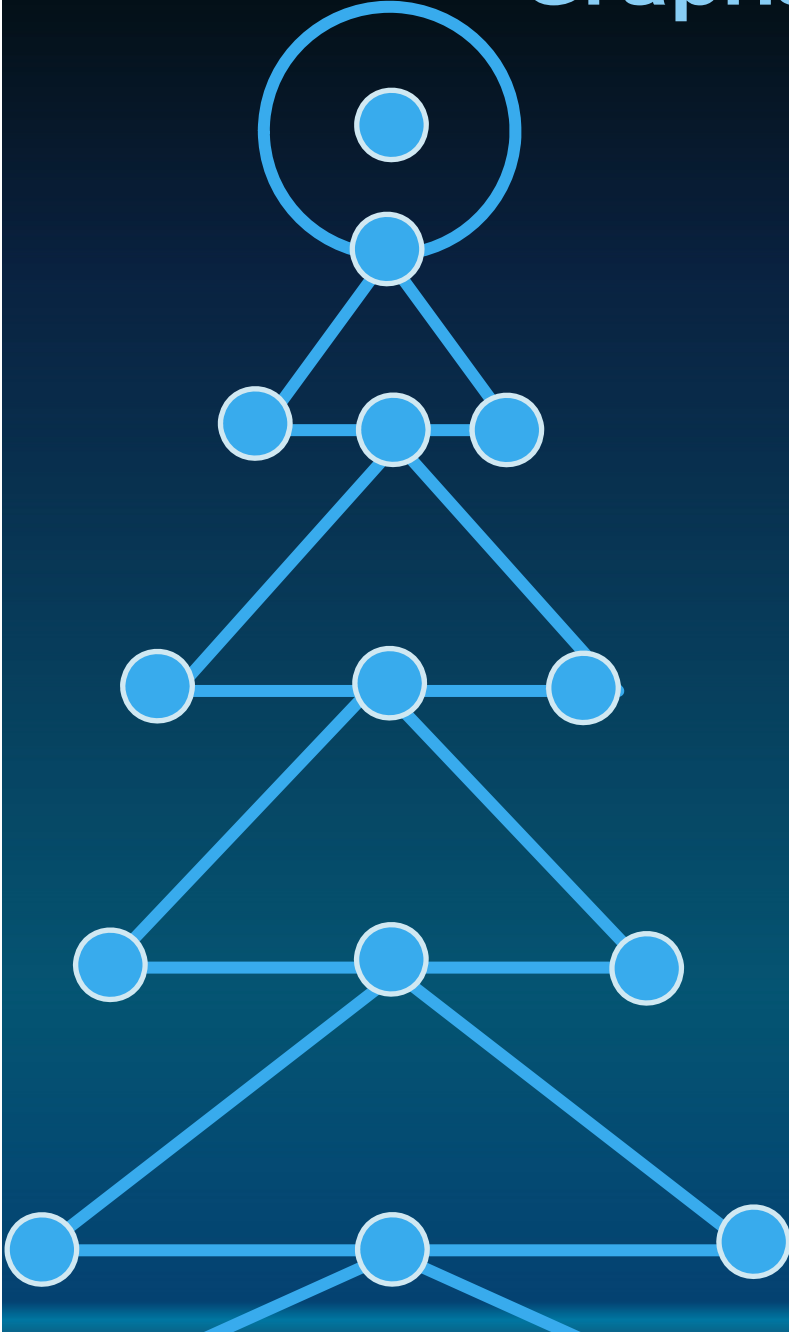
# Graphs and Complexity

## Measures of Complexity

Multifractal parameters

Connectivity index

Complexity index ( $CI$ )



# Graphs and Complexity

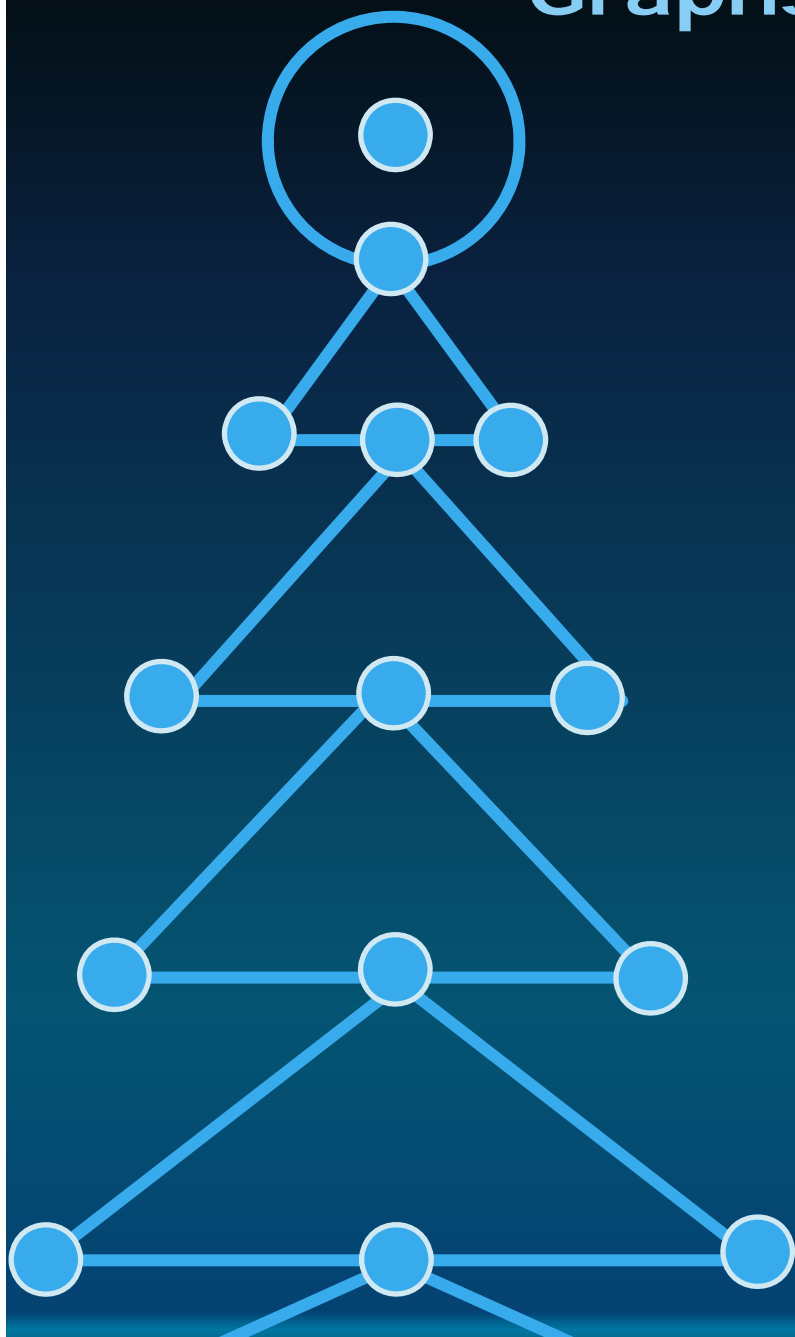
## Measures of Complexity

Multifractal parameters

Connectivity index

Complexity index (CI)

M. Randić, D. Plavšić On the Concept of Molecular Complexity *Croatica Chemica Acta*, 2002, 75 (1) 107



# Graphs and Complexity

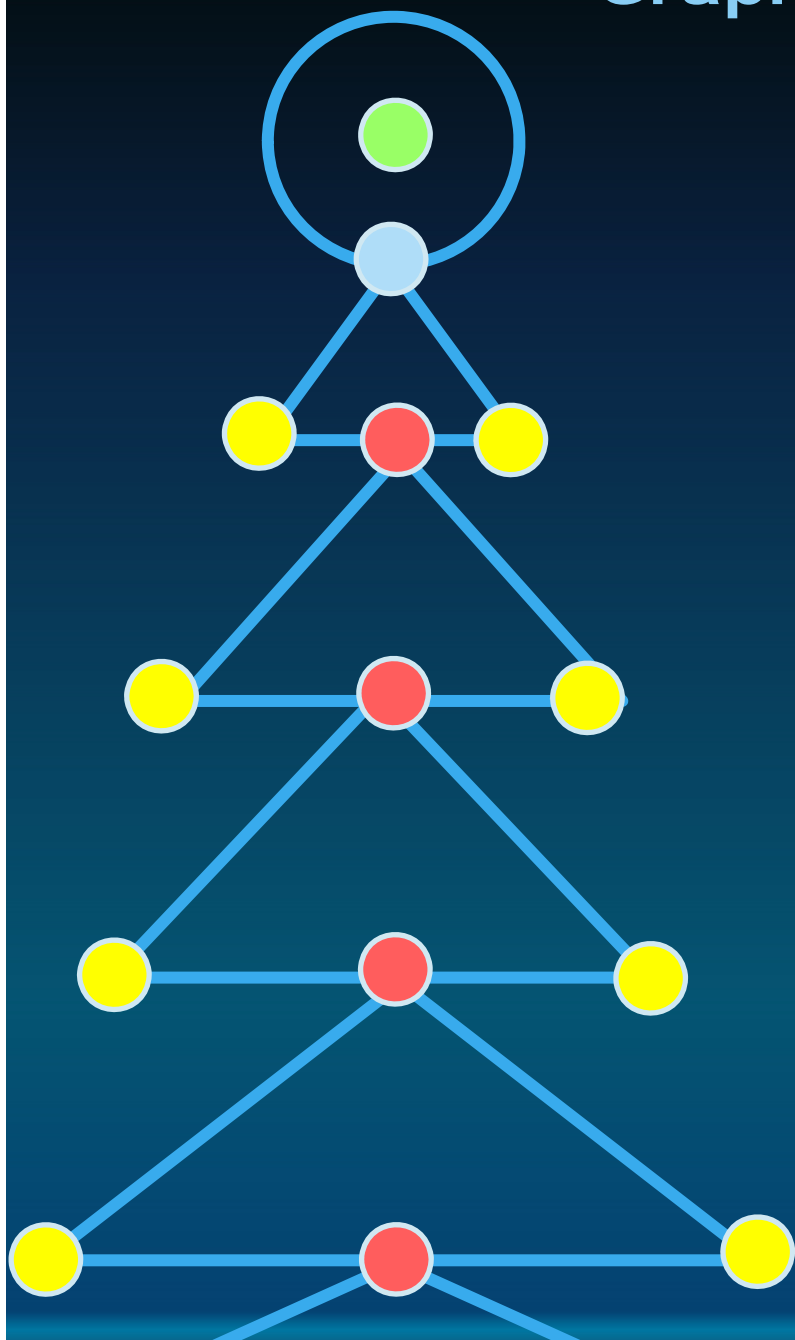
## Measures of Complexity

Multifractal parameters

Connectivity index

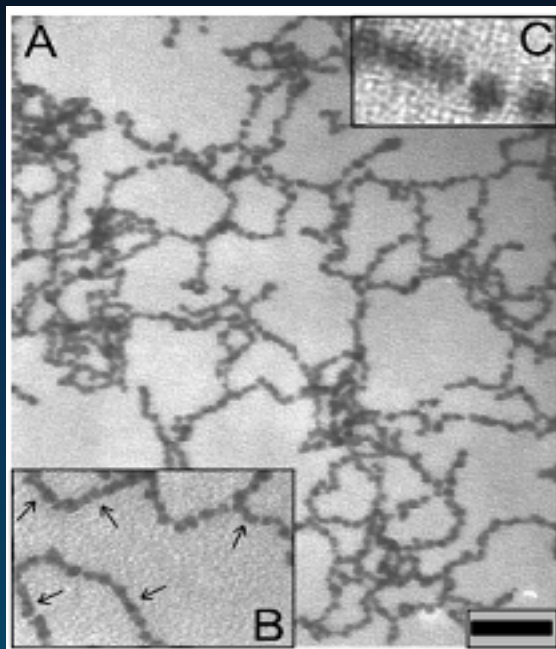
Complexity index (CI)

M. Randić, D. Plavšić On the Concept of Molecular Complexity *Croatica Chemica Acta*, 2002, 75 (1) 107

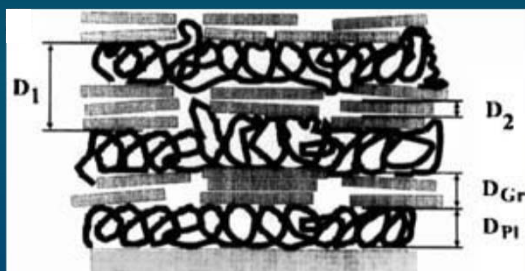




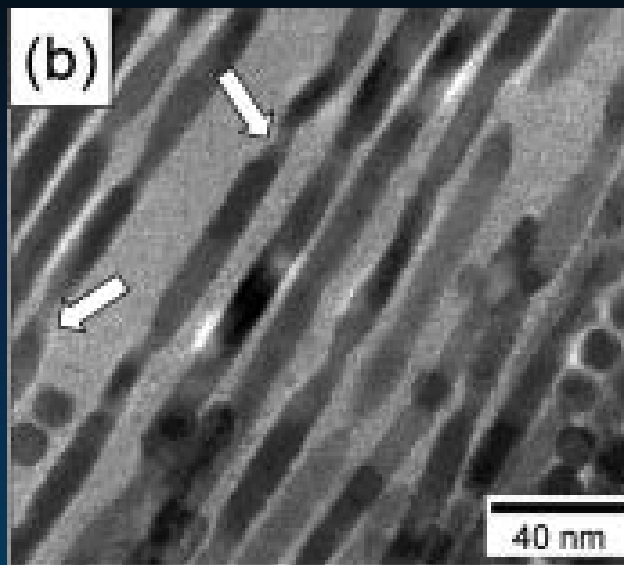
# Nanoassemblies



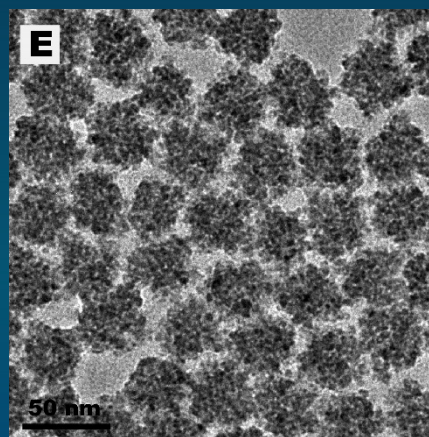
Tang, Z.; Kotov, N. A.; Giersig, M.;  
*Science*, 2002, 297, 237.



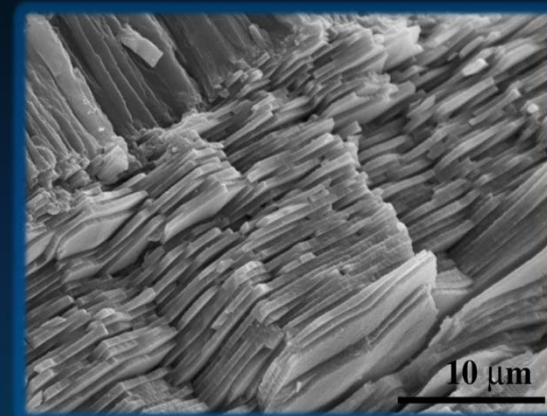
Kotov, N.A.; Dékány, I.; Fendler,  
J.H. *Adv. Mater.* 1996, 8, 637.



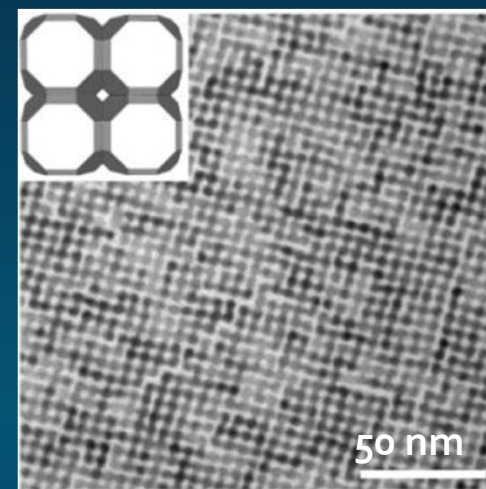
Cho, K.-S.; Talapin, D. V.; Gaschler,  
W. L.; Murray, C. B., *J. Am. Chem.  
Soc.*, 2005, 127, 7140



Y. Xia, T. D. Nguyen, M. Yang, B. Lee, A.  
Santos, P. Podsiadlo, Z. Tang, S. C. Glotzer,  
N. A. Kotov, *Nature Nanotech*, 2011, 6, 580



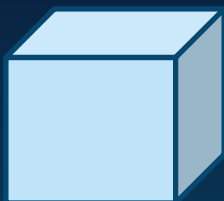
S. Blank, et al.. *J. Microsc.*  
2003, 212, 280.



W. H. Evers, B.Goris, S. Bals,  
M.Casavola, J.de Graaf, R.van  
Roi, M. Dijkstra, D.  
Vanmaekelbergh, *Nano Lett.*  
2013, 13, 2317

# Graph Theory (GT) of Nanoassemblies

**NODES – represent zero-dimensional nanoscale building blocks**

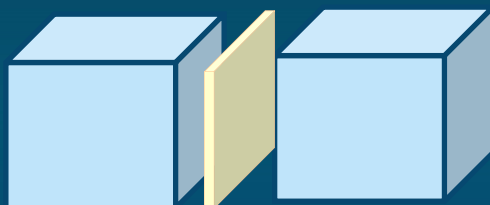


Generalized nanoparticle



$K_1$  graph

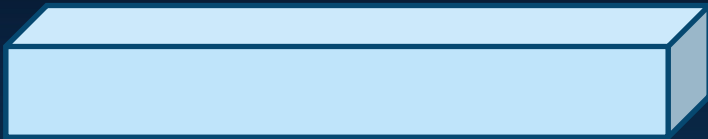
**EDGE - represents organic-inorganic interface**



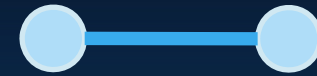
A generalized layer of organic ligands



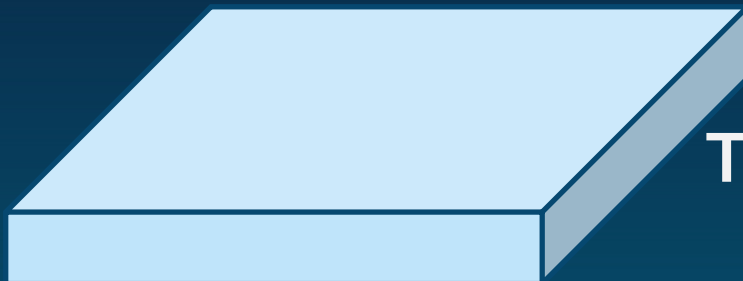
# GT Representation for Complex Building Blocks



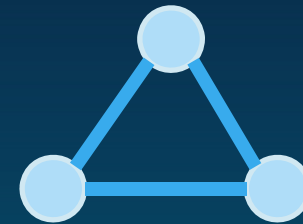
One-dimensional  
nanorod



$K_2$



Two-dimensional  
nanosheet



$K_3$



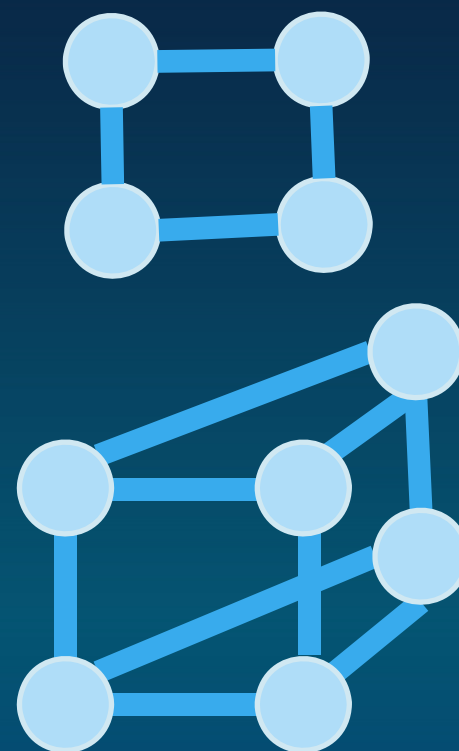
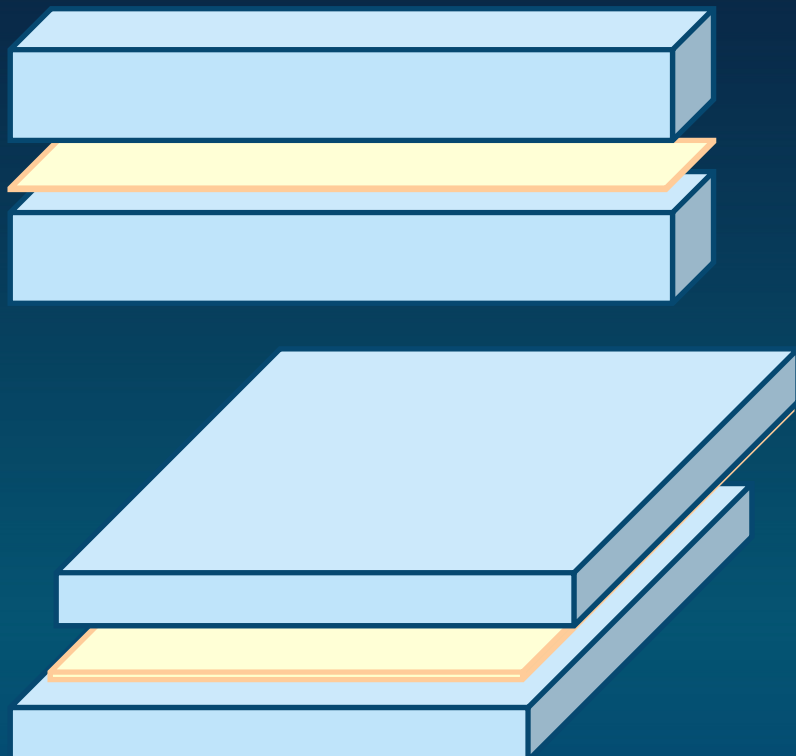
Three-dimensional  
chiral building  
block



$K_5$

# Connectivity Between Complex Blocks

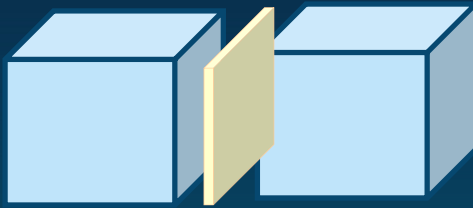
EDGE - represents organic-inorganic interface



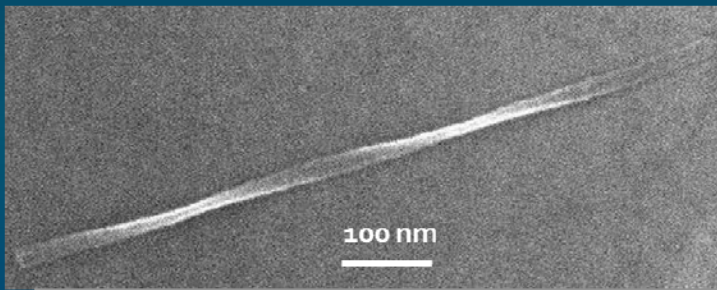
# Calculations of Complexity Index

Number of edges for a node =  $N$

$$CI = N + \sum N \text{ (nearest neighbors)}/2 + \sum N \text{ (next neighbors)}/4 + \dots$$

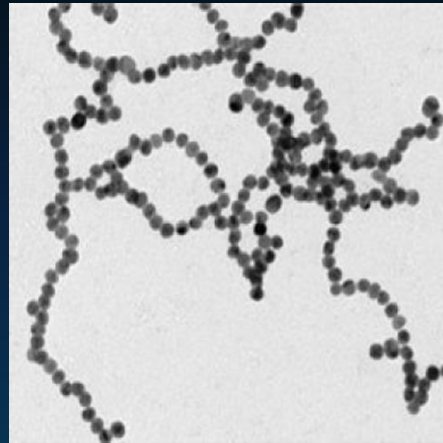
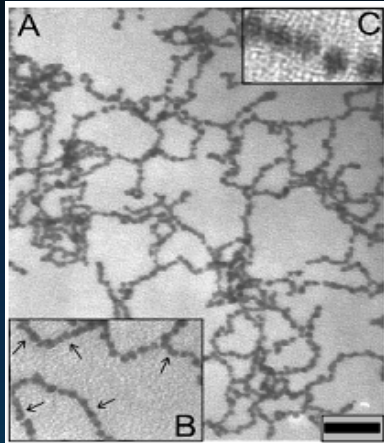


$$CI = 1 + [1/2] = 1.5$$

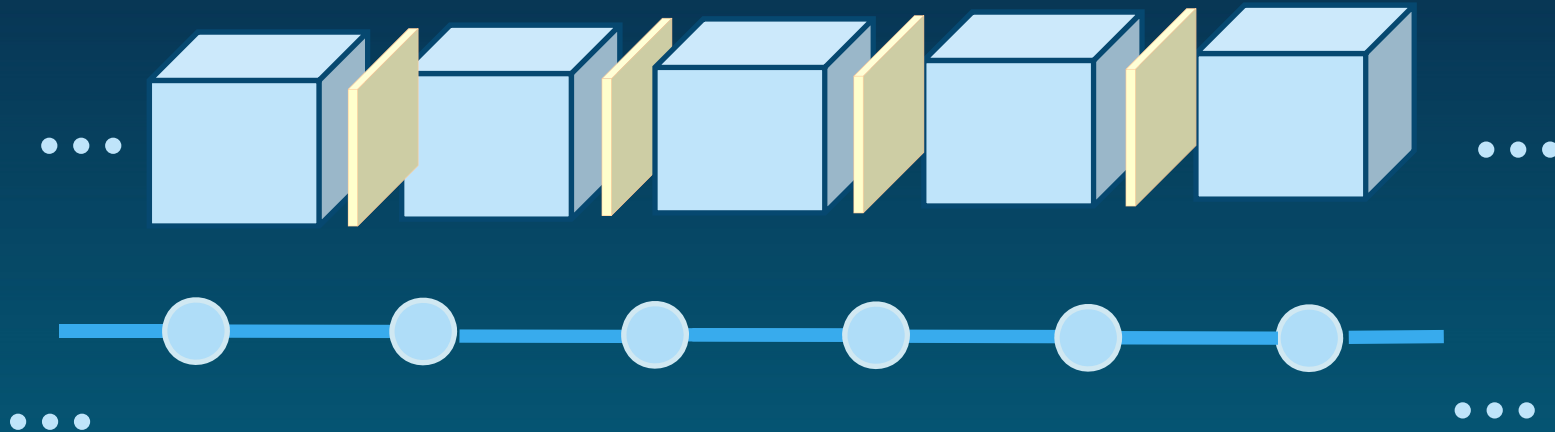


$$CI = 4 + [16/2] = 12$$

# Calculations of Complexity Index



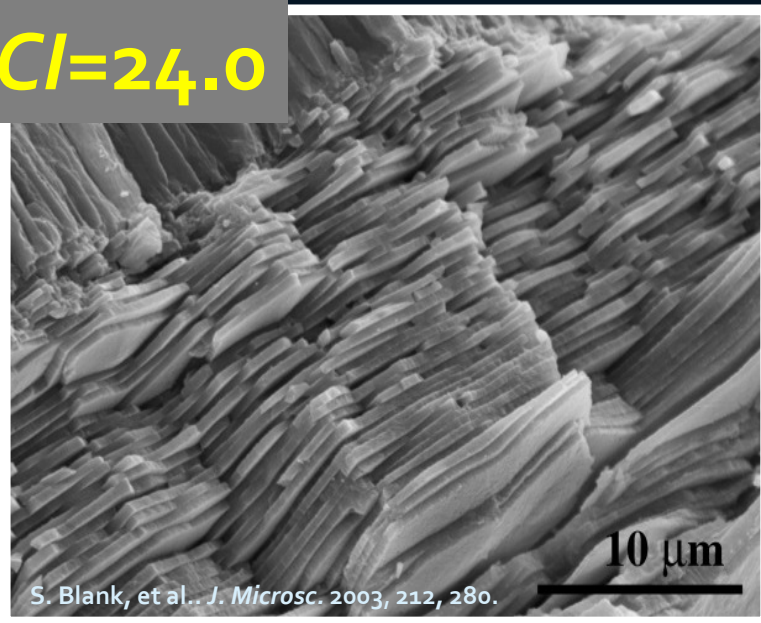
M. Li, S. Johnson, H. Guo, E. Dujardin  
S. Mann, A Generalized Mechanism for  
Ligand-Induced Dipolar Assembly of Plasmonic  
Gold Nanoparticle Chain Networks *Advance Funct.*  
*Mater*, 2011, 21, 851



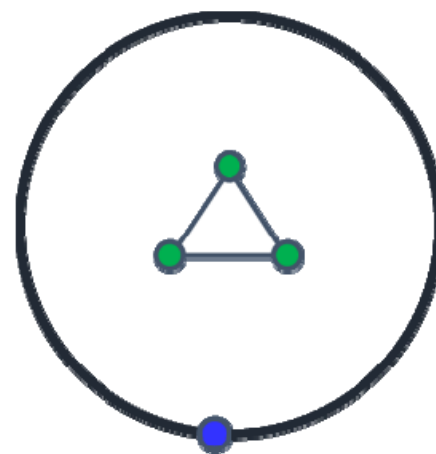
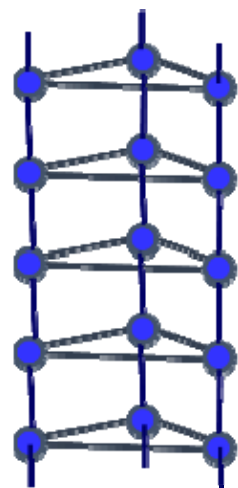
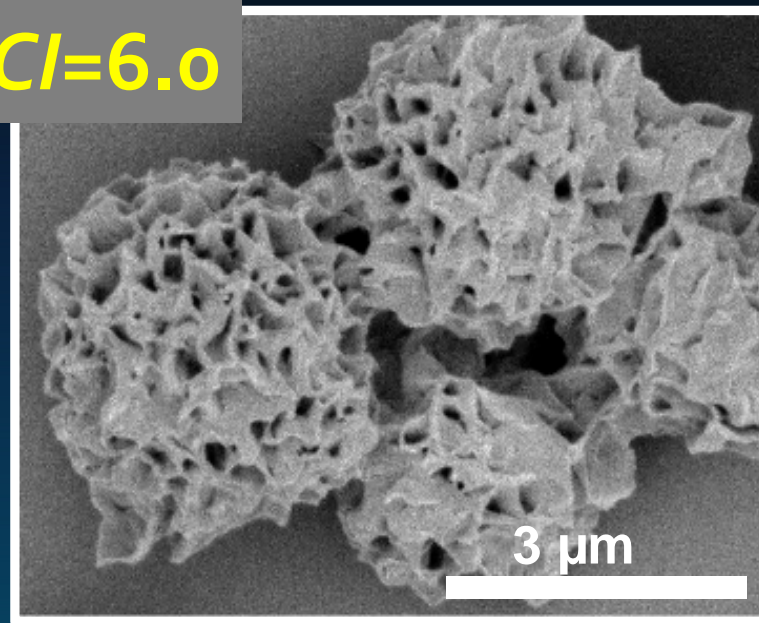
$$CI = 2 + [4/2] + [4/4] + [4/8] + \dots = 2 + \text{Lim}(\sum 4/2^n) = 6$$

# Graph Theory Models

$CI=24.0$

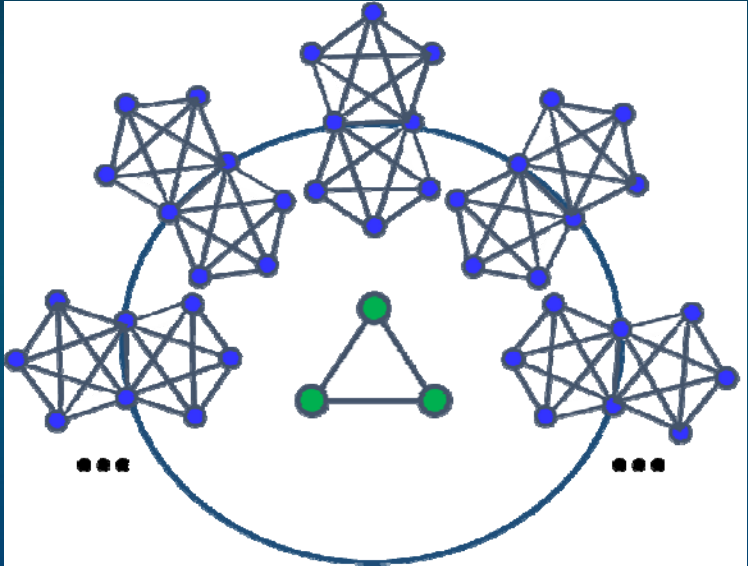
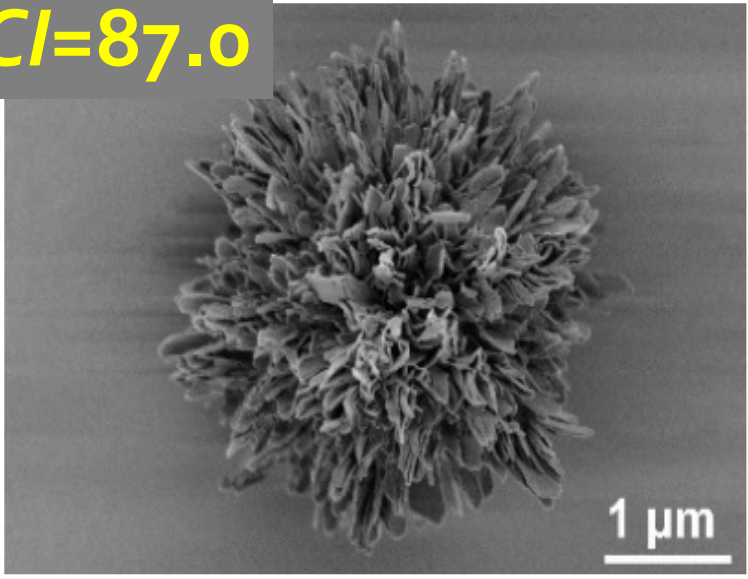


$CI=6.0$

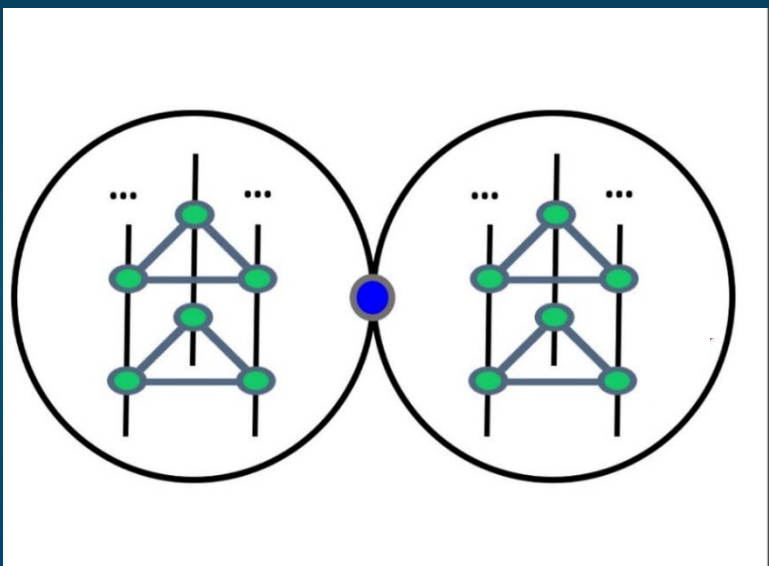
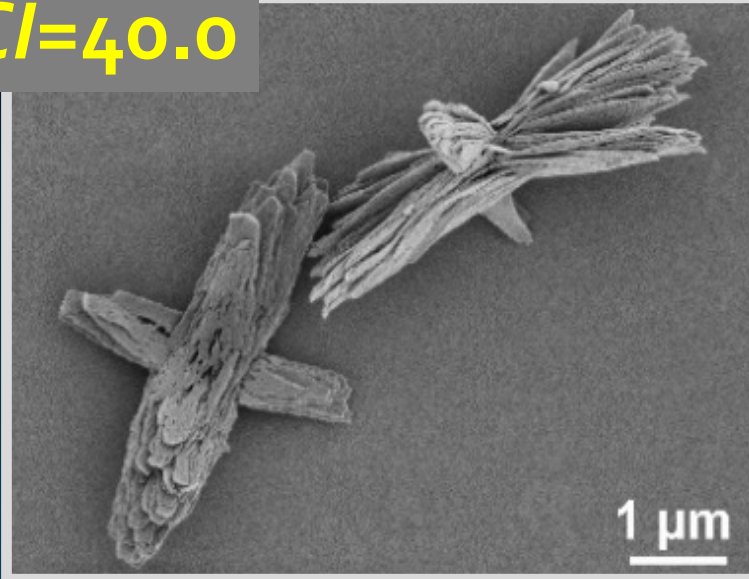


# Graph Theory Models

$Cl=87.0$



$Cl=40.0$





# Thank You!

NIH  
NSF  
DARPA  
ONR

AFOSR  
ARO  
DOE  
DTRA

Dow Chemicals  
Boeing  
Dow Chemicals  
3D Biomatrix

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